



Code Development for Collective Effects

K. Li, H. Bartosik, G. Iadarola, L. Mether, A. Oeftiger,
A. Passarelli, A. Romano, G. Rumolo, M. Schenk

HB2016, 3-8 July, Malmo, Sweden

A large cable-stayed bridge is silhouetted against a bright orange sunset sky. A large, semi-transparent white oval is centered over the bridge, containing the text. The bridge has four tall pylons and numerous stay cables. The foreground shows the bridge's deck and support structure.

CDCE2016!?

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Context:

Collective effects pose **important limitations** in modern **high brightness circular accelerators**. Studying and understanding these effects can help overcoming these limitations.

Numerical methods form one of the **fundamental contemporary tools** used for this purpose. We discuss some modern approaches for numerical modeling of collective effects and show some use-cases employing the example of the **PyHEADTAIL framework**.

Outline:

1. Introduction
2. Basic model of the accelerator-beam system
3. Modern approaches and program architectures
4. Performance considerations
5. Applications, present status and perspectives



Summary:

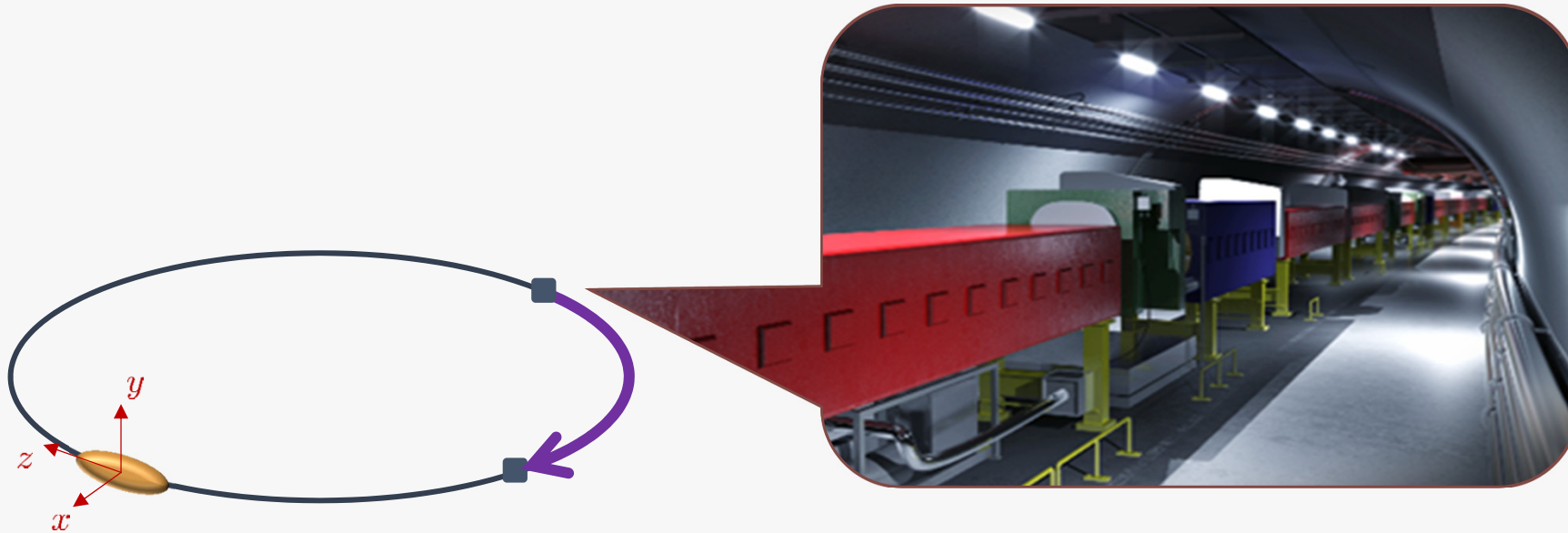
Brief outline of the **nature of collective effects** and why we study them with computer simulation programs.

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Modeling collective effects

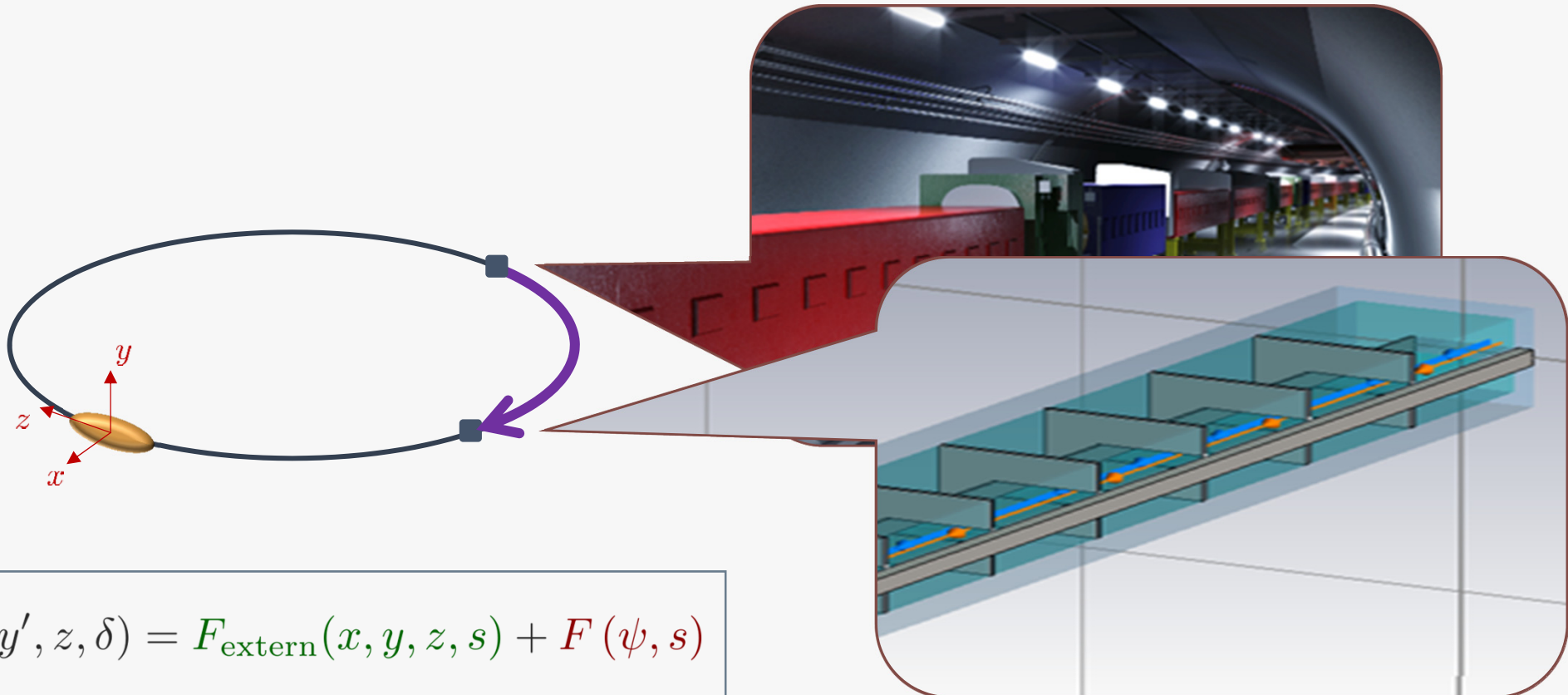
- Beam dynamics deals with studying the **evolution of the phase space variables** i.e., the **generalized coordinates** and **canonically conjugate momenta** of a beam in an accelerator
- Generally this evolution is determined by **external force fields** (magnets, electrostatic fields, RF fields)



$$\frac{d}{dt} \psi(x, x', y, y', z, \delta) = F_{\text{extern}}(x, y, z, s)$$

Modeling collective effects

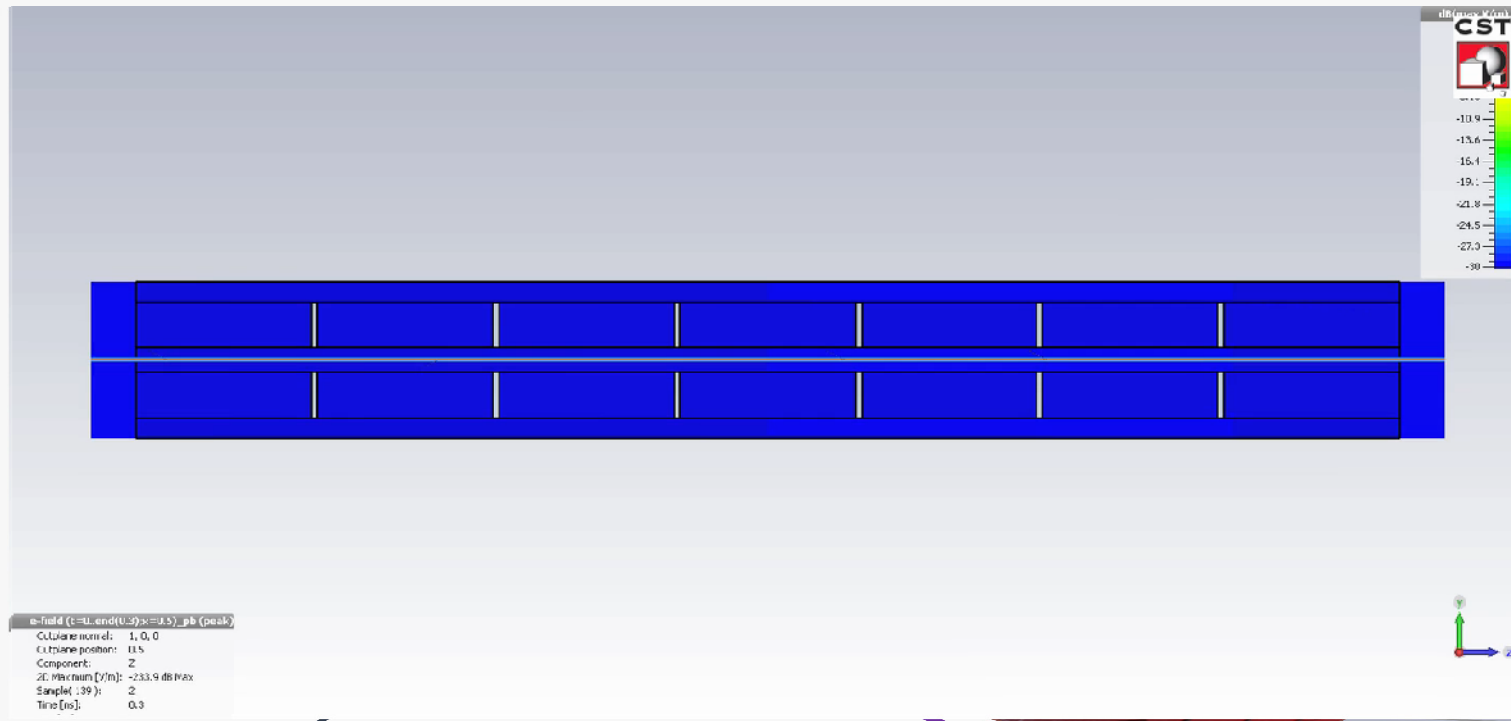
- Beam dynamics deals with studying the **evolution of the phase space variables** i.e., the **generalized coordinates** and **canonically conjugate momenta** of a beam in an accelerator
- Generally this evolution is determined by **external force fields** (magnets, electrostatic fields, RF fields)
- Collective effects add to this fields that depend on the **phase space distribution function** itself (space charge, wake fields)



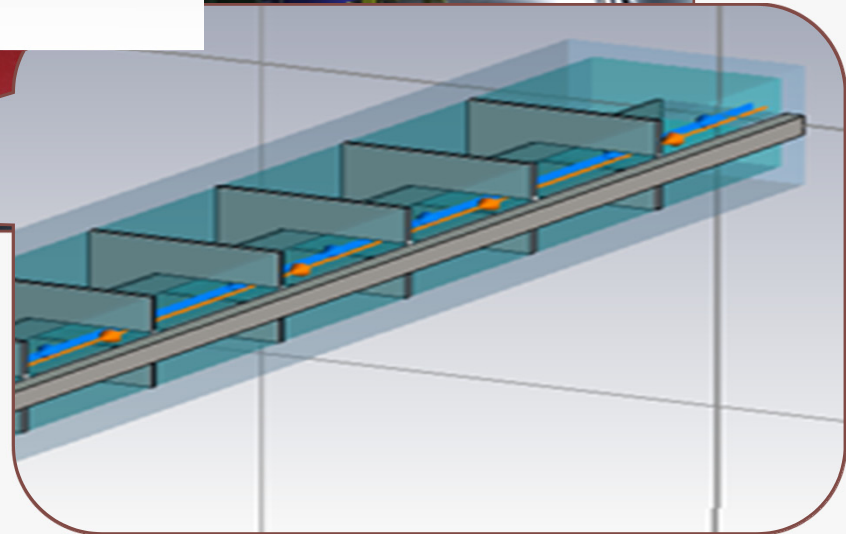
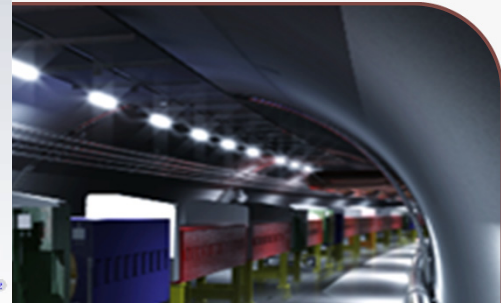
$$\frac{d}{dt} \psi(x, x', y, y', z, \delta) = F_{\text{extern}}(x, y, z, s) + F(\psi, s)$$

Modeling collective effects

-
-
-



s i.e., the **generalized coordinates** and
 rostatic fields, RF fields)
on function itself (space charge, wake

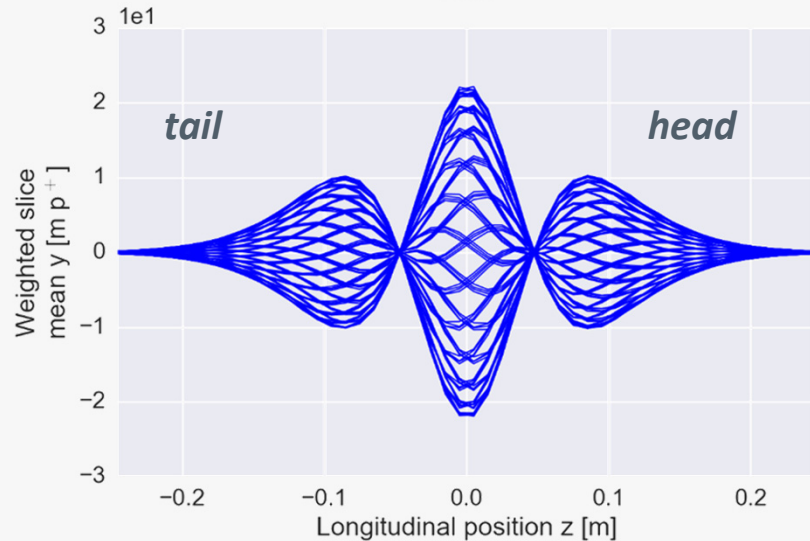
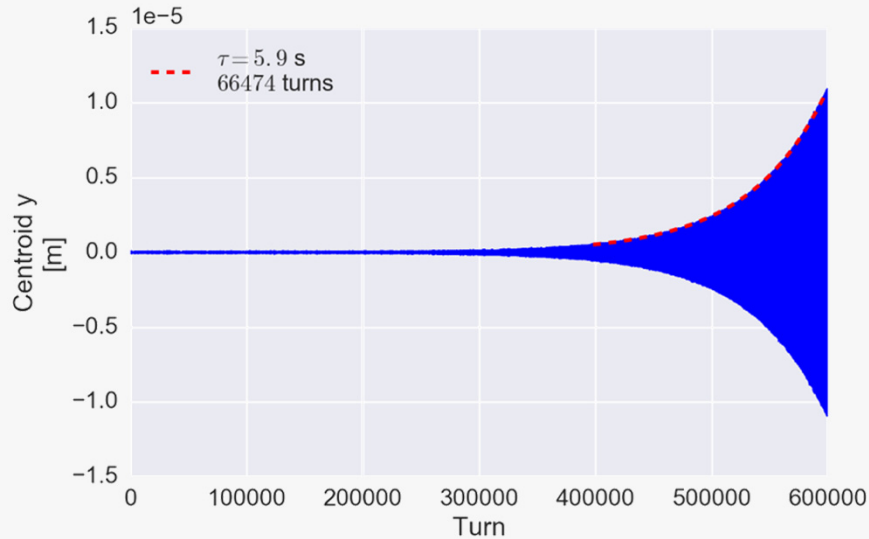


$$\frac{d}{dt} \psi(x, x', y, y', z, \delta) = F_{\text{extern}}(x, y, z, s) + F(\psi, s)$$



Modeling collective effects

- Beam
- Calculations
- Generalized coordinates
- Coherent effects

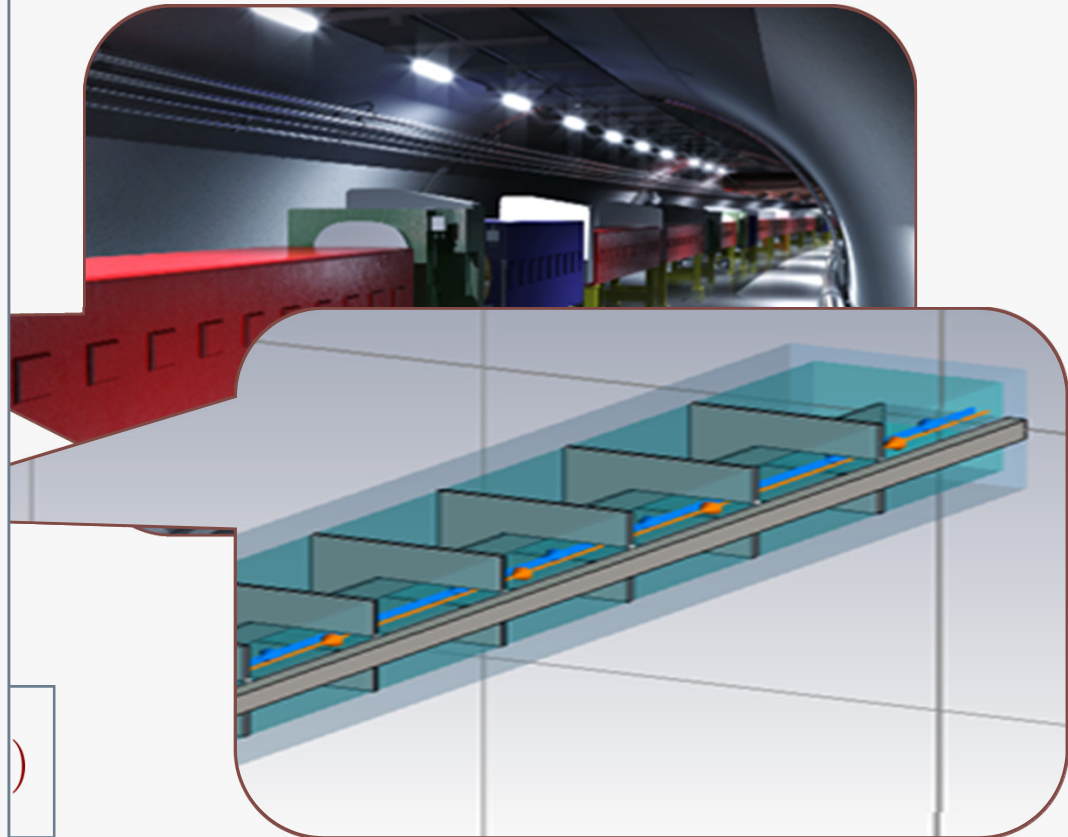


Courtesy Michael Schenk

phase space variables i.e., the generalized coordinates and momenta

fields (magnets, electrostatic fields, RF fields)

phase space distribution function itself (space charge, wake



$$\frac{d}{dt} \psi$$



Modeling collective effects

- Beam dynamics deals with studying the **evolution of the phase space variables** i.e., the **generalized coordinates** and **canonically conjugate momenta** of a beam in an accelerator
- Generally this evolution is determined by **external force fields** (magnets, electrostatic fields, RF fields)
- Collective fields) charge, wake

- For a **multi-particle system** this self-consistency equation becomes arbitrarily complex and practically **impossible to solve**
- Obtaining the **multi-particle dynamics** requires **computer simulation codes**

$$\frac{d}{dt} \psi(x, x', y, y', z, \delta) = F_{\text{extern}}(x, y, z, s) + F(\psi, s)$$

Summary:

Brief explanation of the **numerical modelling** of the accelerator-beam system employed for computer simulation programs to study **collective effects in circular accelerators**.

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Coordinate system



- Bunch acquires and transports information from elements actions (messenger!)
- Elements imprint their action on bunch.

$$\left[\begin{array}{c} (x_i) \\ (x'_i) \end{array} \quad \begin{array}{c} (y_i) \\ (y'_i) \end{array} \quad \begin{array}{c} (z_i) \\ (\delta_i) \end{array} \right]_{i=1, \dots, N} \in \mathbb{R}^{2N}$$

Betatron motion



- Bunch acquires and transports information from elements actions (messenger!)
- Elements imprint their action on bunch.

Chromaticity: coupling to longitudinal

Detuning with amplitude: continuous detuning

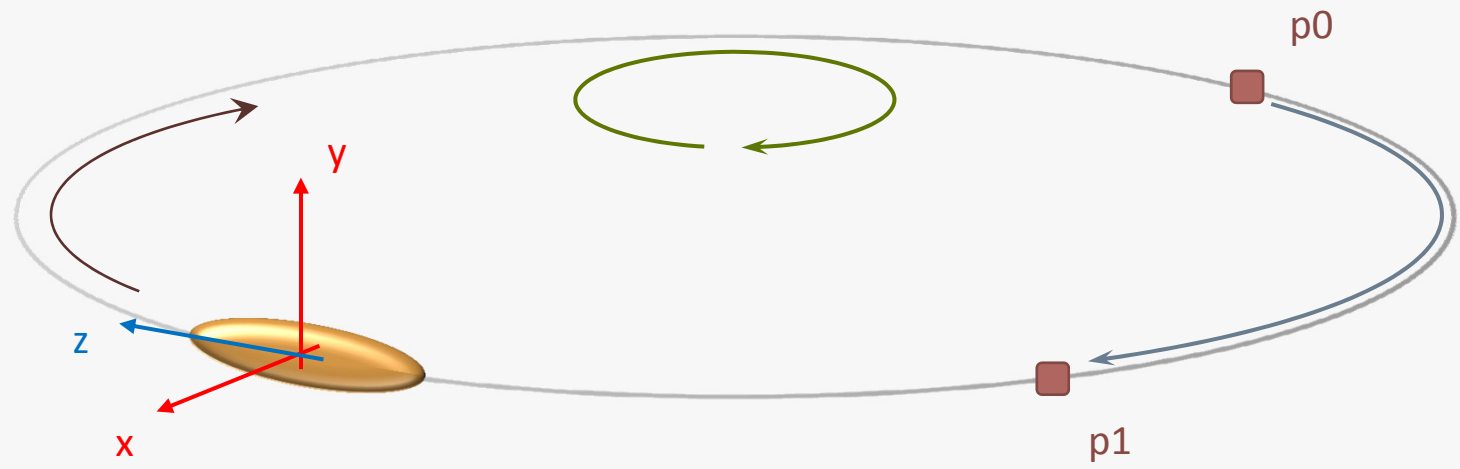
$$\Delta\mu_i \sim \Delta\mu_0 + \left(\xi \delta_i + \alpha_{xx} J_{x,i} + \alpha_{xy} J_{y,i} \right) \frac{\Delta\mu_0}{2\pi Q}$$

$$\mathcal{M}_i = \begin{pmatrix} \sqrt{\beta_1} & 0 \\ -\frac{\alpha_1}{\sqrt{\beta_1}} & \frac{1}{\sqrt{\beta_1}} \end{pmatrix} \begin{pmatrix} \cos(\Delta\mu_i) & \sin(\Delta\mu_i) \\ -\sin(\Delta\mu_i) & \cos(\Delta\mu_i) \end{pmatrix} \begin{pmatrix} \frac{1}{\sqrt{\beta_0}} & 0 \\ \frac{\alpha_0}{\sqrt{\beta_0}} & \sqrt{\beta_0} \end{pmatrix}$$

$$\begin{pmatrix} x_i \\ x'_i \end{pmatrix} \Big|_1 = \mathcal{M}_i \begin{pmatrix} x_i \\ x'_i \end{pmatrix} \Big|_0$$

$i = 1, \dots, N$

Synchrotron motion



- Bunch acquires and transports information from elements actions (messenger!)
- Elements imprint their action on bunch.

$$z_{i,k+1/2} = z_{i,k} - \frac{\eta C}{2} \delta_{i,k}$$

$$\delta_{i,k+1} = \delta_{i,k} + \frac{e V_{RF}}{m \gamma \beta^2 c^2} \sin \left(\frac{2\pi h}{C} z_{i,k+1/2} \right)$$

$$z_{i,k+1} = z_{i,k+1/2} - \frac{\eta C}{2} \delta_{i,k+1}$$

$i = 1, \dots, N$
 k : iteration/turn

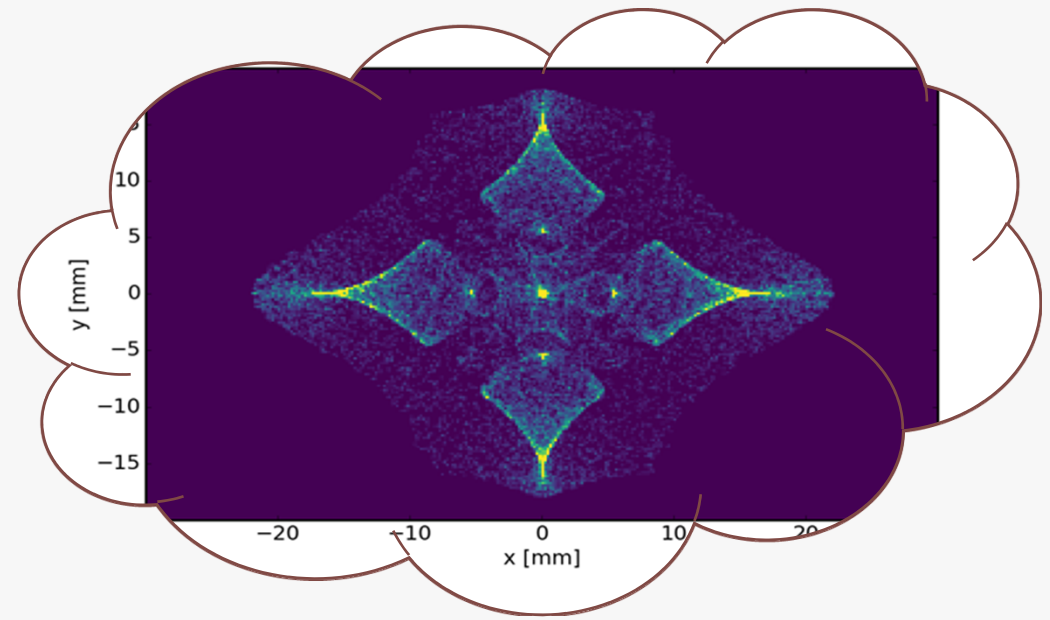
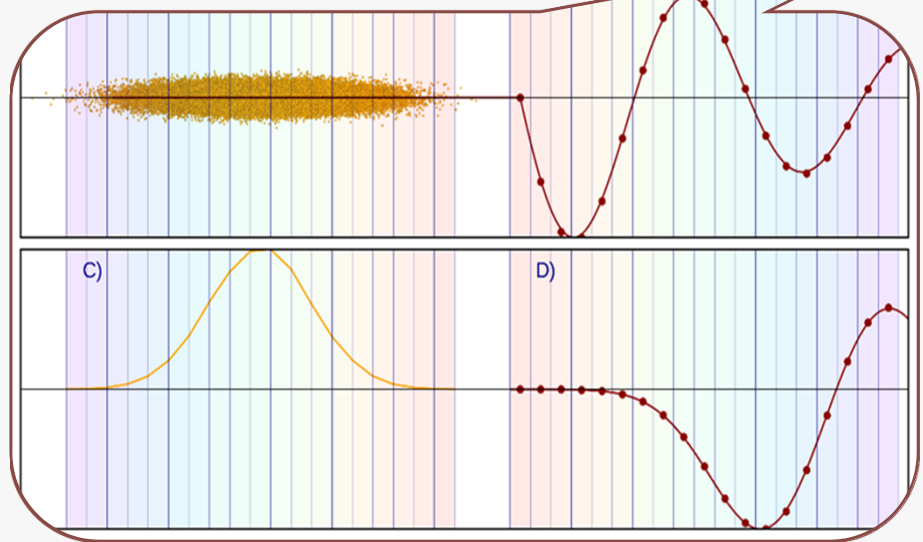
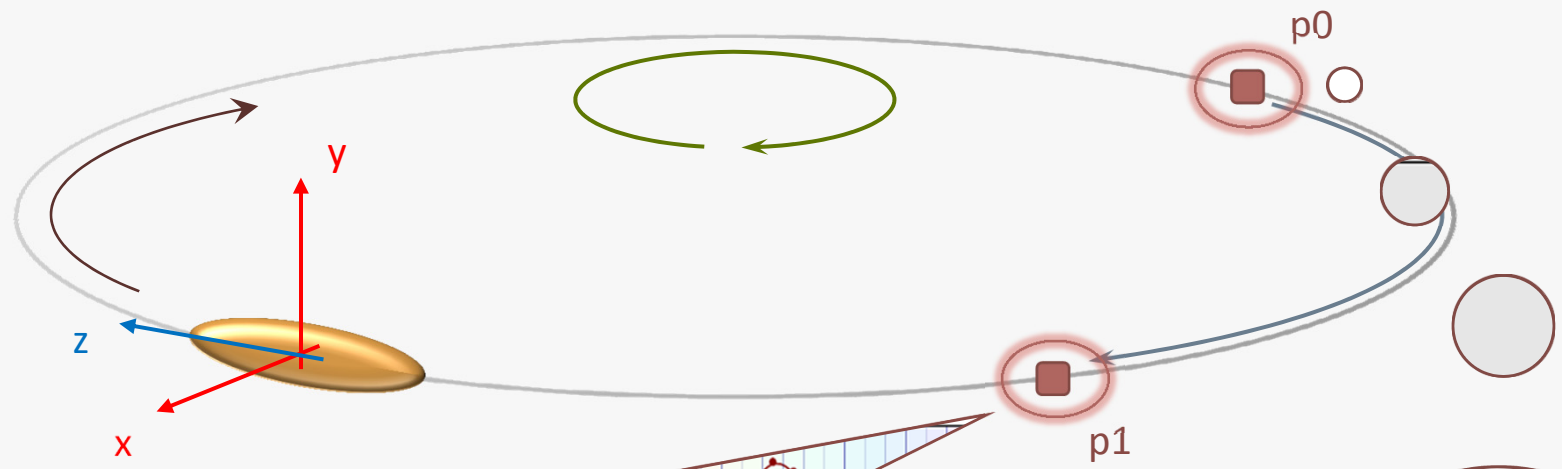
$$z' = -\eta \delta$$

$$\delta' = \frac{e V_{RF}}{m \gamma \beta^2 c^2 C} \sin \left(\frac{2\pi h}{C} z \right)$$

- V_{RF} : RF voltage
- $h = \frac{\omega_{RF}}{\omega_0}$: harmonic number
- ω_0 : Revolution frequency
- C : circumference

Wake fields, e-clouds etc.

- Bunch acquires and transports information from elements actions (messenger!)
- Elements imprint their action on bunch.



Summary:

Some guidelines on programming strategies with their advantages and limitations.

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- What are the demands of modern computer codes?



Simple

- Easy to fix
- Easy to read
- Easy to maintain



Modular

- Easy to extend
- Easy to combine
- Easy to maintain



Dynamic

- Fast
- Flexible
- Interactive

... and each individual module becomes a carefully engineered piece of software.

Be minimalist

- keep number of lines to the minimum necessary

Be pragmatic

- use available libraries and don't re-invent the wheel

Be paranoid

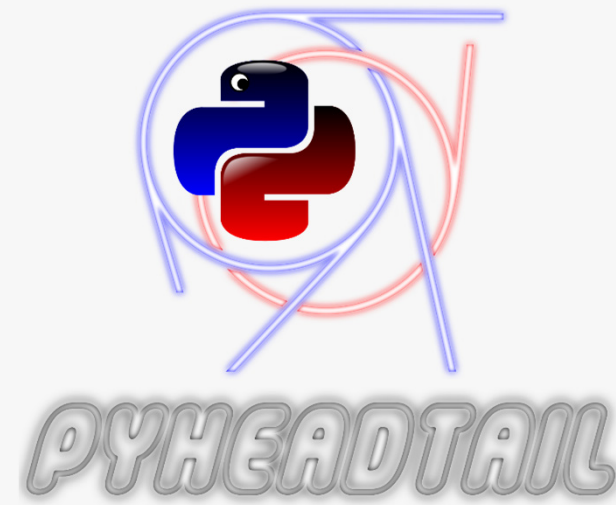
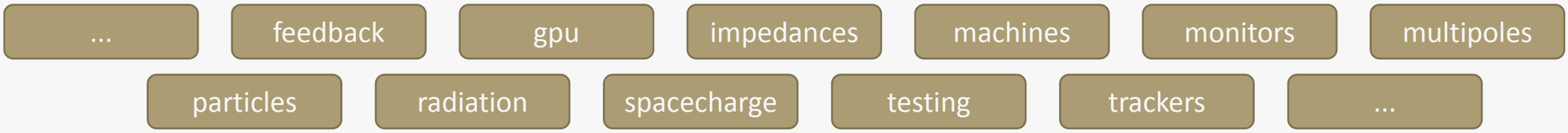
- write clear and well-formatted code

“Always code as if the guy who ends up maintaining your code will be a violent psychopath who knows where you live”

John Woods

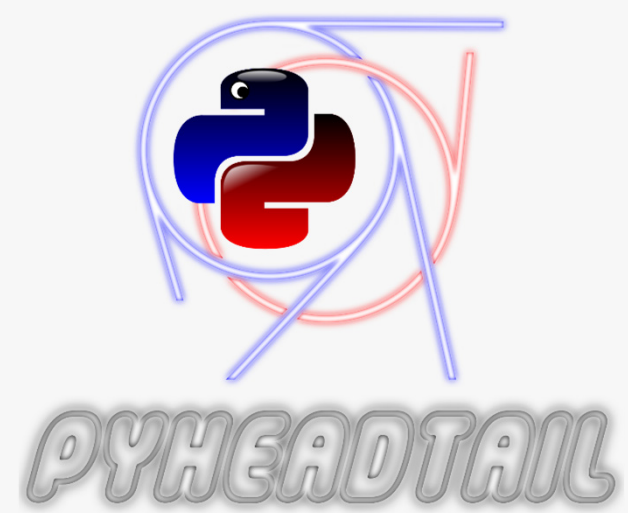
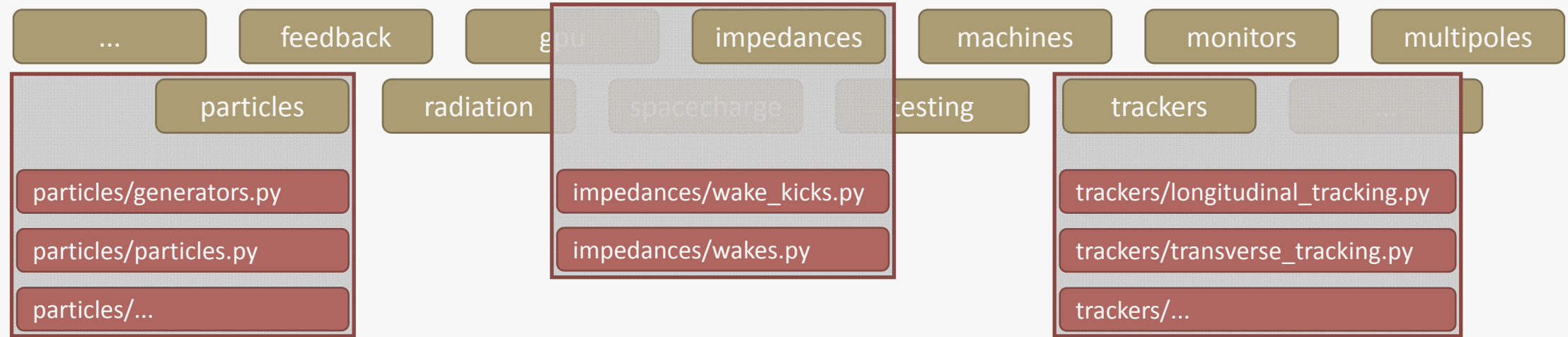


Repository (PyHEADTAIL)

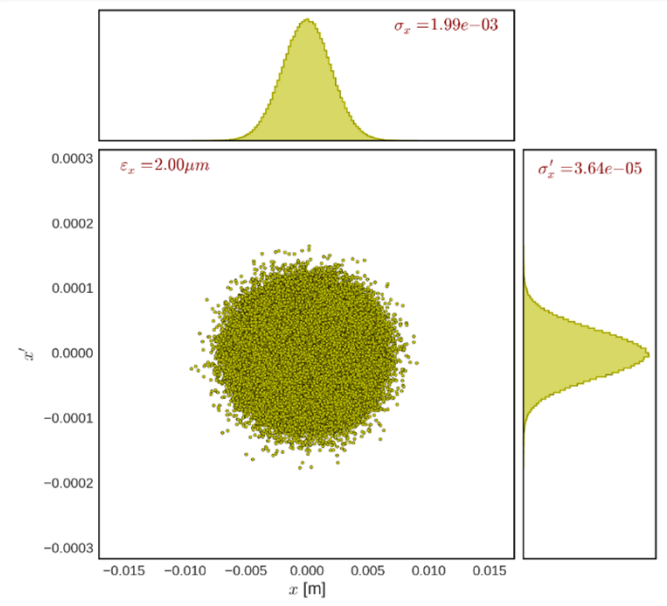
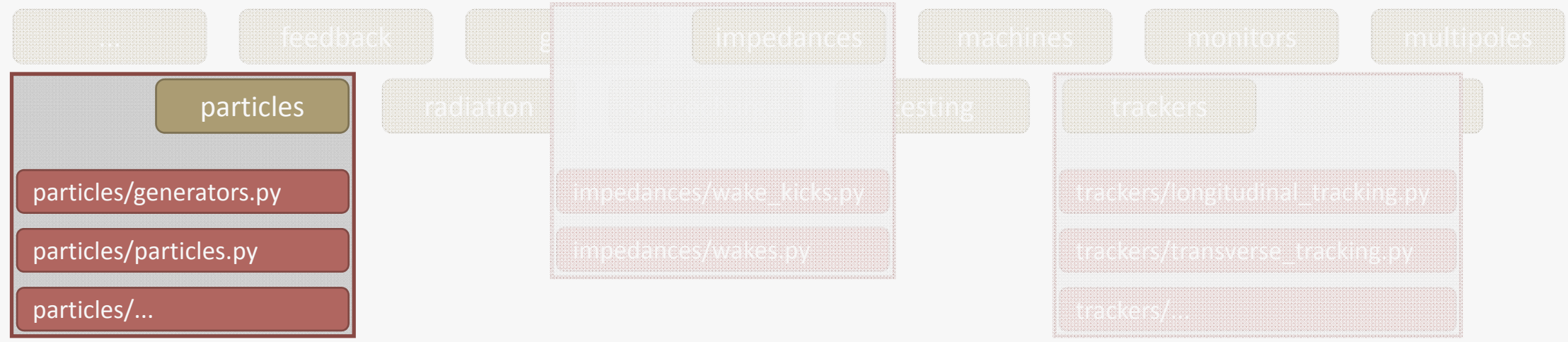




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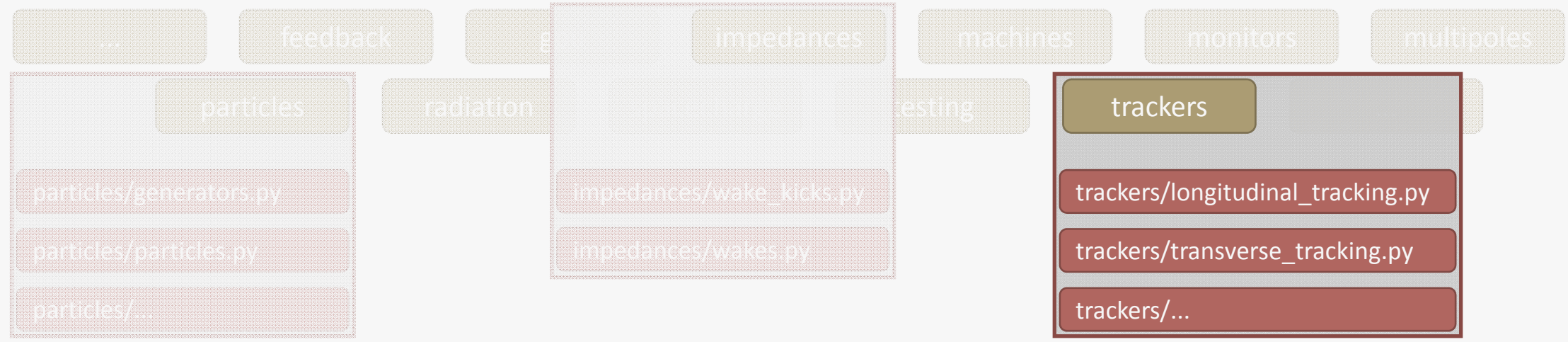


Repository (PyHEADTAIL)

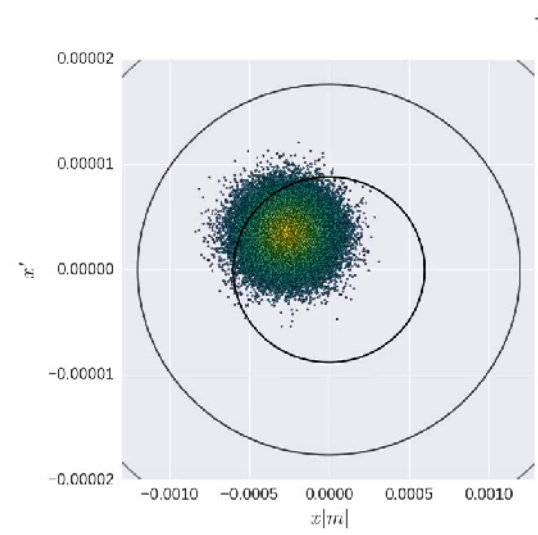


$$\begin{aligned} \epsilon_{\perp} &= \beta\gamma\sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2} \\ &= \beta\gamma\sigma_x\sigma_{x'} \\ \epsilon_{\parallel} &= 4\pi\sigma_z\sigma_{\delta}\frac{p_0}{e} \end{aligned}$$

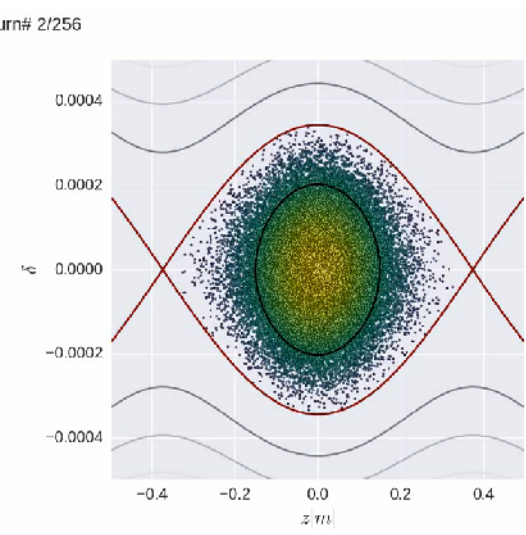
Repository (PyHEADTAIL)



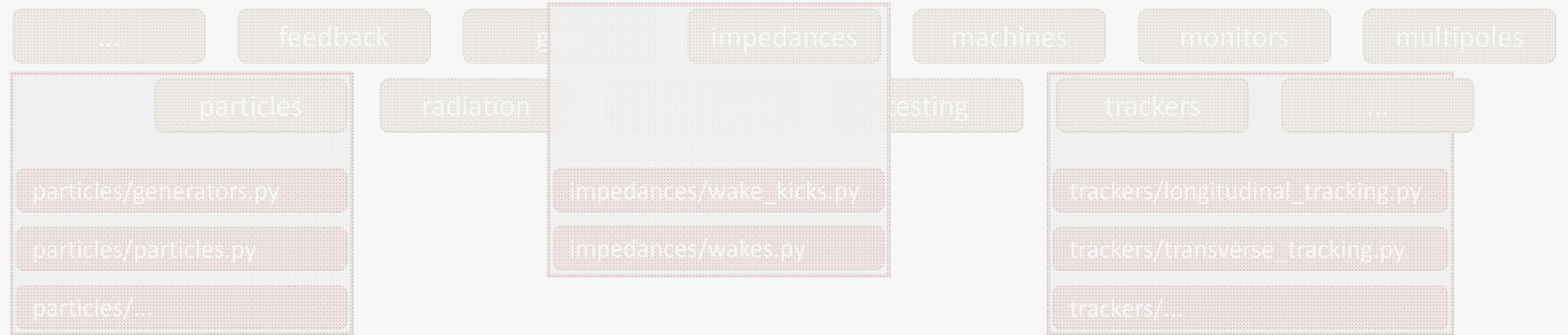
Transverse



Longitudinal



Repository (PyHEADTAIL)



“Just as Code Style, API Design, and Automation are essential for a healthy development cycle, Repository structure is a crucial part of your project’s architecture.”
The Hitchhiker’s Guide to Python

A good repository structure forms the backbone of a project. Object-oriented programming adds to this a defined programming structure.

Building the simulation



Building the simulation

e-cloud - dipole

beam

diagnostics

e-cloud - quad

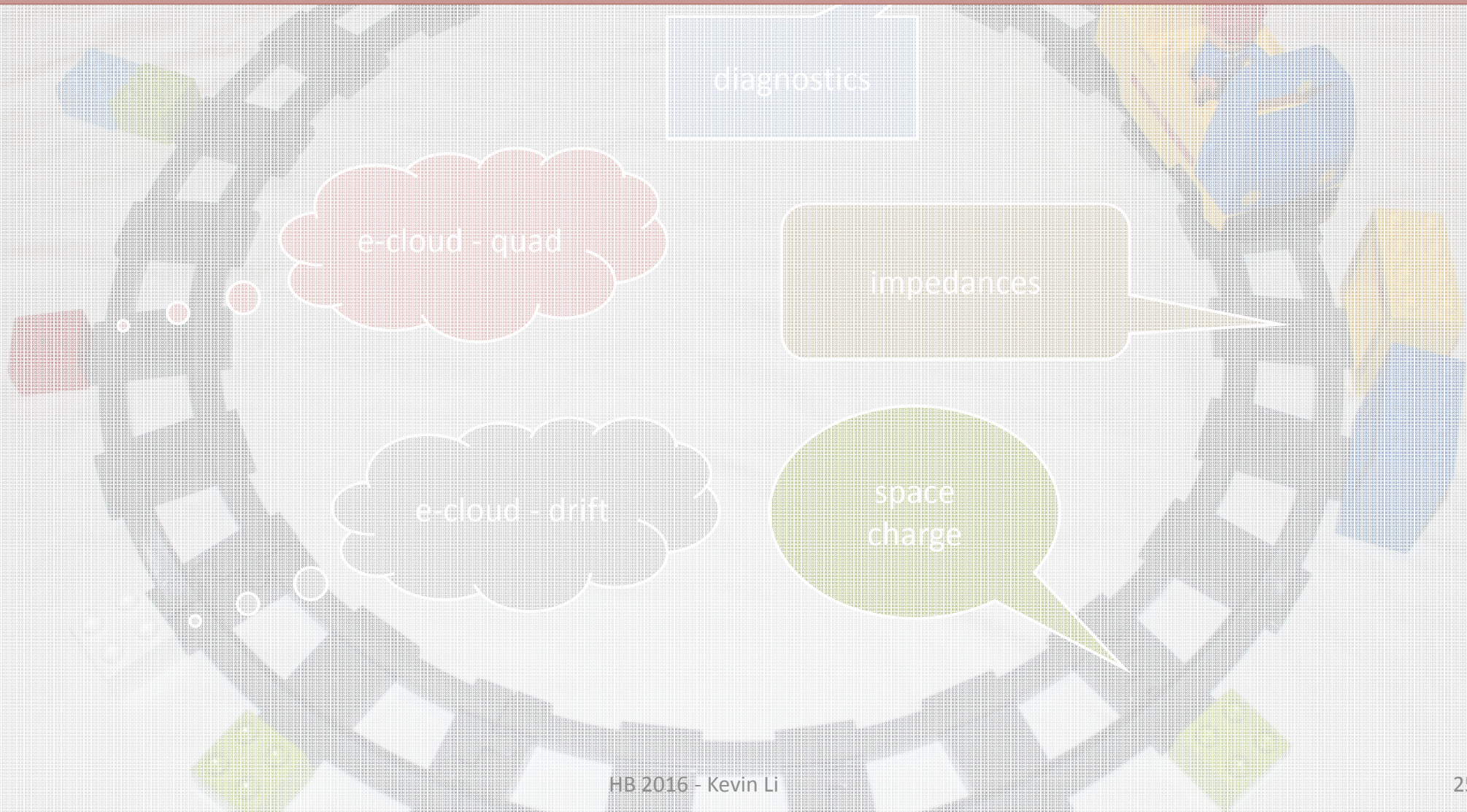
impedances

e-cloud - drift

space charge

With the modular design it becomes easy to design customized simulations.

We need to think of a clever inputfile language that reflects this modularity (example of MAD-X, MAFIA etc.).



~~We need to think of a clever inputfile language that reflects this modularity (example of MAD-X, MAFIA etc.).~~

Why invent yet another language/syntax when there are established and popular languages most programmers already know:

*“It was nice to learn Python;
a nice afternoon.”*

Donald Knuth

Input file becomes simply **a Python script** → inject the full power of the Python programming language to the input file

- Control flows
- Third party libraries
- Data analysis and visualization
- ...

Setting up a simulation becomes writing a small program/script – simple, highly customizable, interactive

Import modules

Choice of parameters

Instantiate objects

Assemble ring

Tracking loop –
scriptable with
Python control flows

See backup slides

```
File Edit Options Buffers Tools Python Virtual Envs Elpy YASnippet Help
166
167 s_cnt = 0
168 n_turns = 256
169 monitorswitch = False
170
171 print '\n--> Begin tracking \n'
172
173 for i in range(n_turns):
174     t0 = time.clock()
175     for m in one_turn_map:
176         m.track(bunch)
177
178     bunchmonitor.dump(bunch)
179
180     if not monitorswitch:
181         if (bunch.mean_x() > 1e3 or bunch.mean_y() > 1e3 or i > n_turns-8192):
182             print "-> Monitor"
183             monitorswitch = True
184
185             if s_cnt < 8192:
186                 slicemonitor.dump(bunch)
187                 s_cnt += 1
188
189     if (i+1) % 1 is not 0:
190         continue
191
192     Jx = np.sqrt((bunch.x-bunch.mean_x())**2 +
193                (transverse_map.beta_x[0] * (bunch.xp-bunch.mean_xp()))**2)
194     ax1.contour(XX, YY, JJ, 6, lw=1)
195     ax1.scatter(bunch.x, bunch.xp, c=Jx, cmap=plt.cm.viridis_r, s=6)
196     ax2.contour(ZZ, PP, HH, 6, lw=1)
197     ax2.contour(ZZ, PP, HH, levels=[0], colors='darkred', lw=3)
198     ax2.scatter(bunch.z, bunch.dp, c=rfbucket.hamiltonian(bunch.z, bunch.dp),
199                cmap=plt.cm.viridis, s=6)
200     ax1.set_xlim(-1.3e-3, 1.3e-3)
201     ax1.set_ylim(-2e-5, 2e-5)
202     ax2.set_xlim(-.5, .5)
203     ax2.set_ylim(-5e-4, 5e-4)
204     ax1.set_xlabel("$x [m]$", fontsize=24)
205     ax1.set_ylabel("$x'$", fontsize=24)
206     ax2.set_xlabel("$z [m]$", fontsize=24)
207     ax2.set_ylabel("$\delta$", fontsize=24)
```

Summary:

Some ideas and examples how to improve performance limitations encountered when working with interpreted languages (Python).

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An important hitch remains on the **FAST** requirement:

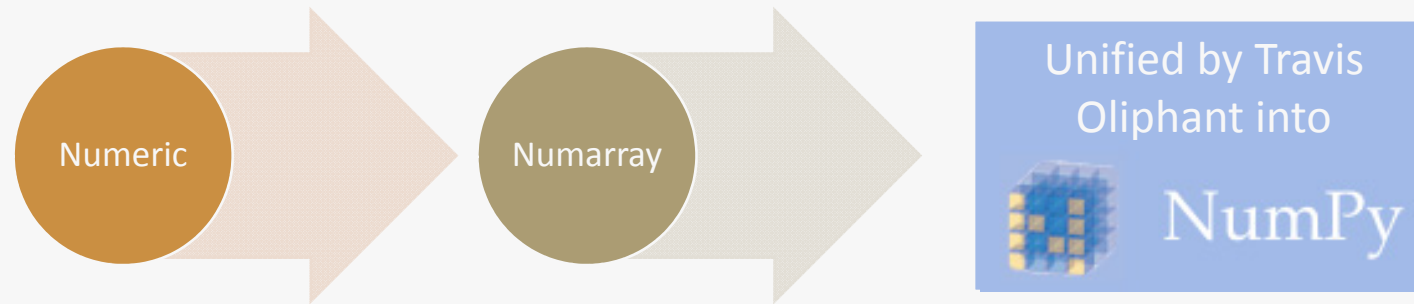
“Python was not made to be fast... .. but to make developers fast.”

*Writing faster Python,
Sebastian Witowski*

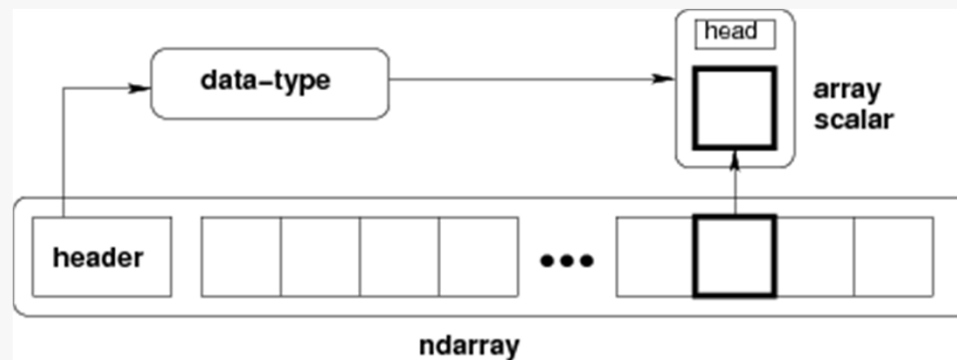
Being an interpreted language, strongly but dynamically typed, **Python can be slow in execution!** This needs to be handled.

Python used as it is usually is slow for number crunching!

In the late 90s the Python scientific community worked on bringing the computationally intensive parts to a lower level:



The core functionality of NumPy is its "ndarray", for n -dimensional array, data structure.



Today, NumPy is the unrivaled basis for nearly all scientific tools in Python.



A very simple example for speed-up

- Profile the evaluation of the sine function over an array
- x is an array with 6M entries ranging uniformly from 0 to 2 pi

012b_optimisation_example Last Checkpoint: 4 hou

File Edit View Insert Cell Kernel Help

Profile

```
%timeit pysin(x)
%timeit npsin(x)
%timeit cmsin(x, a)
```

1 loop, best of 3: 171 ms per loop

012b_optimisation_example Last Checkpoint: 4 minutes ago (autosaved)

File Edit View Insert Cell Kernel Help

Python sin

for loop in Python – never do this!

```
In [4]: def pysin(x):
        y = [math.sin(i) for i in x]
        return y
```





A very simple example for speed-up

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012b_optimisation_example Last Checkpoint: 4 hou

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```
%timeit pysin(x)
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%timeit cmsin(x, a)
```

1 loop, best of 3: 171 ms per loop
10 loops, best of 3: 26.4 ms per loop

PYHEADTAIL notebook

012b_optimisation_example Last Checkpoint: 4 minutes ago (autosaved)

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Python sin

```
In [4]: def pysin(x):
        y = [math.sin(i) for i in x]
        return y
```

Numpy sin

```
In [5]: import numpy as np
        def npsin(x):
            return np.sin(x)
```

Vectorization: the array is interpreted by NumPy and the loop is executed at C level





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Small low-level extensions for Python accessing native Python data structures – core coding in Python

012b_optimisation_example Last Checkpoint: 11 minutes ago (unsaved ch

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Generated by Cython 0.23.4

Yellow lines hint at Python interaction. Click on a line that starts with a "+" to see the C code that Cython genera

```
01:
+02: import numpy as np
03: cimport numpy as np
04: cimport cython
05: from cython.parallel import prange
06: from libc.math cimport sin
07:
08: @cython.boundscheck(False)
09: @cython.wraparound(False)
10: @cython.cdivision(False)
+11: def cmsin(double[:,1] x, double[:,1] s):
12:
+13:     cdef int n = x.shape[0]
14:     cdef int i
+15:     for i in prange(n, nogil=True, num_threads=4):
+16:         s[i] = sin(x[i])
```

Typed Memoryviews: efficient data access and handling

Explicit loop at C level; yellow lines indicate Python overhead





A very simple example for speed-up

- Profile the evaluation of the sine function over an array
- x is an array with 6M entries ranging uniformly from 0 to 2 pi





Profile

```
%timeit pysin(x)
%timeit npsin(x)
%timeit cmsin(x, a)

1 loop, best of 3: 171 ms per loop
10 loops, best of 3: 26.4 ms per loop
10 loops, best of 3: 26.8 ms per loop

%timeit vdt_sin(x, a)
%timeit vdt_sinv(x, a)
%timeit vdt_sincos(x, a, b)

100 loops, best of 3: 11 ms per loop
100 loops, best of 3: 8.23 ms per loop
100 loops, best of 3: 17.2 ms per loop
```

012b_optimisation_example Last Checkpoint: 8 minutes ago (autosaved)

Small low-level extensions for Python

Python accessing native Python data structures — core coding in Python

Import from an external library and use it in Cython

(here, vdtmath:
D. Piparo et al. 2014 J. Phys.: Conf. Ser. 513 052027
"Speeding up HEP experiment software with a library of fast and auto-vectorisable mathematical functions")

```

File Edit View Insert Cell Kernel Help
Generated by Cython 0.23.4

Yellow lines hint at Python interaction.
Click on a line that starts with a "+" to see the C code that Cython generates.

+01: #export LD_LIBRARY_PATH=$LD_LIBRARY_PATH:/home/.../lib
02: #cython boundscheck=False
03:
04: cimport cython
+05: import numpy as np
06: cimport numpy as np
07: from cython.parallel import prange
08:
09: cdef extern from "sin.h" namespace "vdt":
10:     cdef double fast_sin(double x) nogil
11:     cdef void fast_sinv(int n, double *x, double *s) nogil
12:
13: cdef extern from "sincos.h" namespace "vdt":
14:     cdef void fast_sincos(double x, double &s, double &c) nogil
15:
16: @cython.boundscheck(False)
+17: def vdt_sin(double[:,1] x, double[:,1] s):
18:
19:     cdef int n = x.shape[0]
20:     cdef int i
21:     for i in prange(n, nogil=True, num_threads=1):
22:         s[i] = fast_sin(x[i])
23:
24: @cython.boundscheck(False)
+25: def vdt_sincos(double[:,1] x, double[:,1] s, double[:,1] c):
26:
27:     cdef int n = x.shape[0]
28:     cdef int i
29:     for i in prange(n, nogil=True, num_threads=1):
30:         fast_sincos(x[i], s[i], c[i])
31:
32: @cython.boundscheck(False)
+33: def vdt_sinv(double[:,1] x, double[:,1] s):
34:
35:     cdef int n = x.shape[0]
36:     fast_sinv(n, &x[0], &s[0])

```





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012b_optimisation_example Last Checkpoint: 4 hou

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```

```
100 loops, best of 3: 11 ms per loop
100 loops, best of 3: 8.23 ms per loop
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```



012b_optimisation_example Last Checkpoint: 8 minutes ago (autosaved)

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Generated by Cython 0.23.4

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```
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02: #cython boundscheck=False
03:
04: cimport cython
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08:
09: cdef extern from "sin.h" namespace "vdt":
10:     cdef double fast_sin(double x) nogil
11:     cdef void fast_sinv(int n, double *x, double *s) nogil
12:
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22:         s[i] = fast_sin(x[i])
23:
24: @cython.boundscheck(False)
+25: def vdt_sincos(double[:,1] x, double[:,1] s, double[:,1] c):
26:
27:     cdef int n = x.shape[0]
28:     cdef int i
+29:     for i in prange(n, nogil=True, num_threads=1):
30:         fast_sincos(x[i], s[i], c[i])
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34:
35:     cdef int n = x.shape[0]
+36:     fast_sinv(n, &x[0], &s[0])
```



Small low-level extensions for

Import from an external library and use it in Cython

(here, vdtmath:
D. Piparo et al. 2014 J. Phys.: Conf. Ser. 513 052027
"Speeding up HEP experiment software with a library of fast and auto-vectorisable mathematical functions")

OpenMP multithreading parallelization; move from e.g. 1 to 4 threads





A very simple example for speed-up

- Profile the evaluation of the sine function over an array
- x is an array with 6M entries ranging uniformly from 0 to 2 pi



012b_optimisation_example Last Checkpoint: 4 hou

File Edit View Insert Cell Kernel Help

Profile

```
%timeit psin(x)
%timeit npsin(x)
%timeit cmsin(x, a)
```

```
1 loop, best of 3: 176 ms per loop
10 loops, best of 3: 26.4 ms per loop
100 loops, best of 3: 13 ms per loop
```

```
%timeit vdt_sin(x, a)
%timeit vdt_sinv(x, a)
%timeit vdt_sincos(x, a, b)
```

```
100 loops, best of 3: 6.12 ms per loop
100 loops, best of 3: 8.19 ms per loop
100 loops, best of 3: 8.26 ms per loop
```



012b_optimisation_example Last Checkpoint: 8 minutes ago (autosaved)

File Edit View Insert Cell Kernel Help

Generated by Cython 0.23.4

```
Yellow lines hint at Python interaction.
Click on a line that starts with a "+" to see the C code that Cython uses.
+01: #export LD_LIBRARY_PATH=$LD_LIBRARY_PATH:/home/.../lib64
02: #cython boundscheck=False
03:
04: cimport cython
+05: import numpy as np
06: cimport numpy as np
07: from cython.parallel import prange
08:
09: cdef extern from "sin.h" namespace "vdt":
10:     cdef double fast_sin(double x) nogil
11:     cdef void fast_sinv(int n, double *x, double *s) nogil
12:
13: cdef extern from "sincos.h" namespace "vdt":
14:     cdef void fast_sincos(double x, double &s, double &c) nogil
15:
16: @cython.boundscheck(False)
+17: def vdt_sin(double[:,1] x, double[:,1] s):
18:
19:     cdef int n = x.shape[0]
20:     cdef int i
+21:     for i in prange(n, nogil=True, num_threads=4):
22:         s[i] = fast_sin(x[i])
23:
24: @cython.boundscheck(False)
+25: def vdt_sincos(double[:,1] x, double[:,1] s, double[:,1] c):
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OpenMP multithreading parallelization; move from e.g. 1 to 4 threads





A very simple example for speed-up



Profile the evaluation of the sine

There are an abundance of tools out there for embedding and extending Python:

CPython API, ctypes, f2py, SWIG, Boost::Python, Numexpr, Cython, PyCUDA, Numba, cffi...

Today, Cython provides a very most modern and flexible approach. However the world is changing fast. Writing simple (and little) code will enable us to remain adaptable.

```
%timeit psin(x)
%timeit npsin(x)
%timeit cmsin(x, a)
```

1 loop, best of 3: 176 ms per loop
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```
%timeit vdt_sin(x, a)
%timeit vdt_sinv(x, a)
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```

100 loops, best of 3: 6.12 ms per loop
100 loops, best of 3: 8.19 ms per loop
100 loops, best of 3: 8.26 ms per loop

```
17: def vdt_sin(double[:,1] x, double[:,1] s):
18:
19:     cdef int n = x.shape[0]
20:     cdef int i
21:     for i in prange(n, nogil=True, num_threads=4):
22:         s[i] = fast_sin(x[i])
23:
24: @cython.boundscheck(False)
25: def vdt_sincos(double[:,1] x, double[:,1] s, double[:,1] c):
26:
27:     cdef int n = x.shape[0]
28:     cdef int i
29:     for i in prange(n, nogil=True, num_threads=1):
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33: def vdt_sinv(double[:,1] x, double[:,1] s):
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36:     fast_sinv(n, &x[0], &s[0])
```

move from e.g. 1 to 4 threads



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unctions")

lization;





A very simple example for speed-up



• Profile the evaluation of the sine

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```
%timeit psin(x)
%timeit npsin(x)
%timeit cmsin(x,
```

1 loop, best of
10 loops, best of
100 loops, best

```
%timeit vdt_sin(
%timeit vdt_sinv
%timeit vdt_sinc
```

100 loops, best
100 loops, best
100 loops, best of 3: 8.26 ms per loop

```
+17: def vdt_sin(double[:,1] x, double[:,1] s):
```

move from e.g. 1 to 4 threads

The next Travis Oliphant:
"Yep. Theano, Numba, numexpr, Cython and PyPy shall one day all merge to form Numtron, defender of sanity, runner of fast numerics."
Dave Warde-Farley

```
32: @cython.boundscheck(False)
+33: def vdt_sinv(double[:,1] x, double[:,1] s):
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```

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Summary:

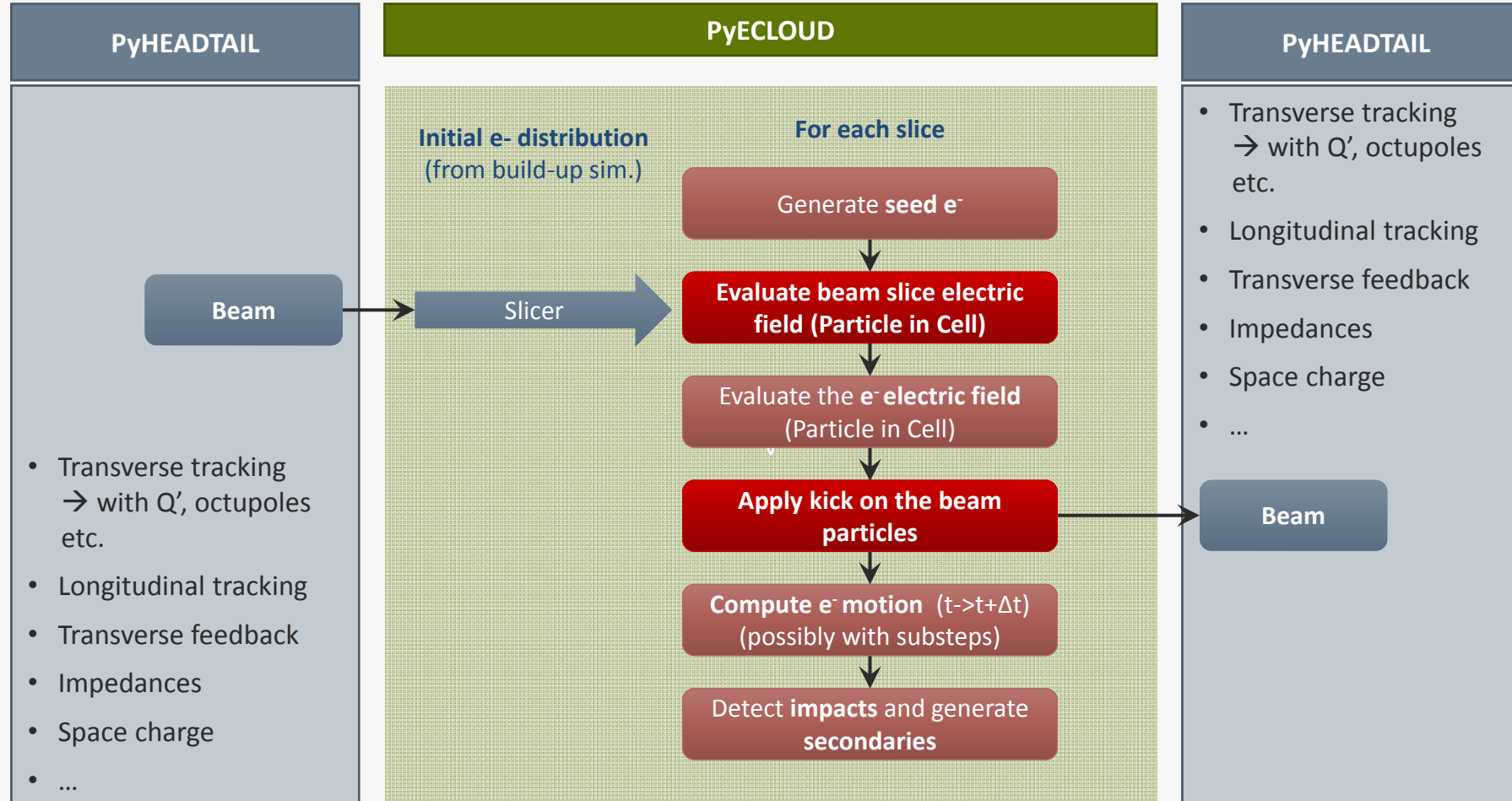
Illustration of a few examples which exploit the architecture and design promoted earlier.

Outline:

1. Introduction
2. Basic model of the accelerator-beam system
3. Modern approaches and program architectures
4. Performance considerations
5. Applications, present status and perspectives

Interfacing with PyPIC and PyELCLOUD

- A self-consistent treatment requires the combination of an instability and a build-up code
- Becomes easily possible with modular structure and good design of codes (e.g. object orientation)

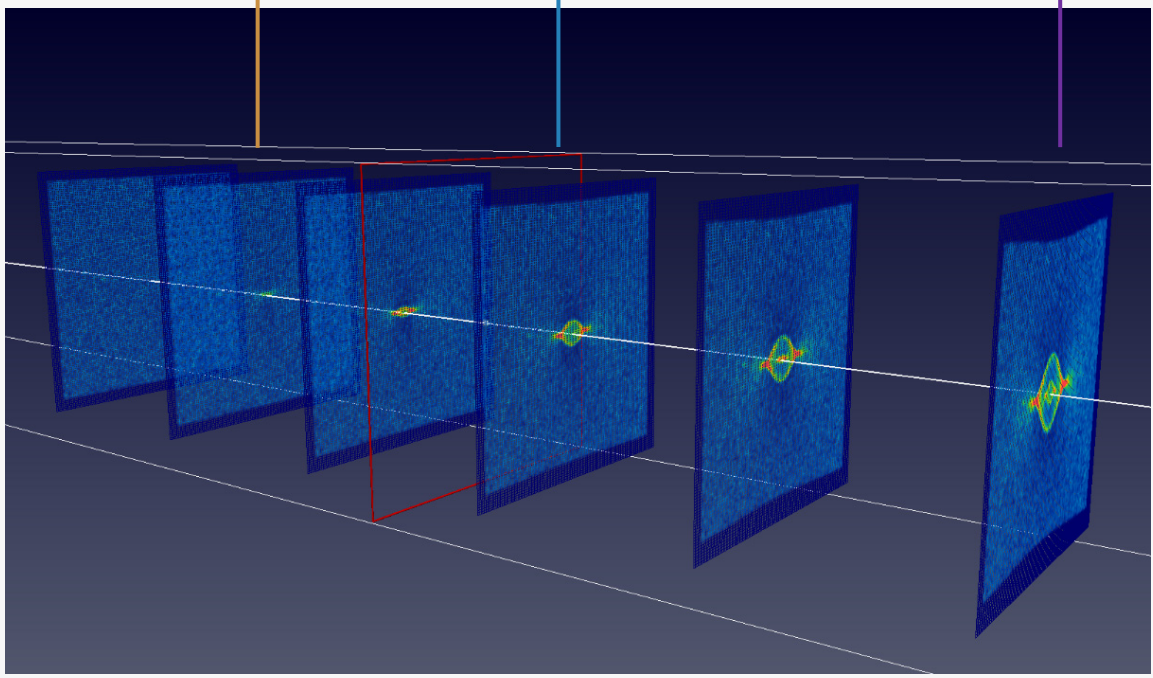
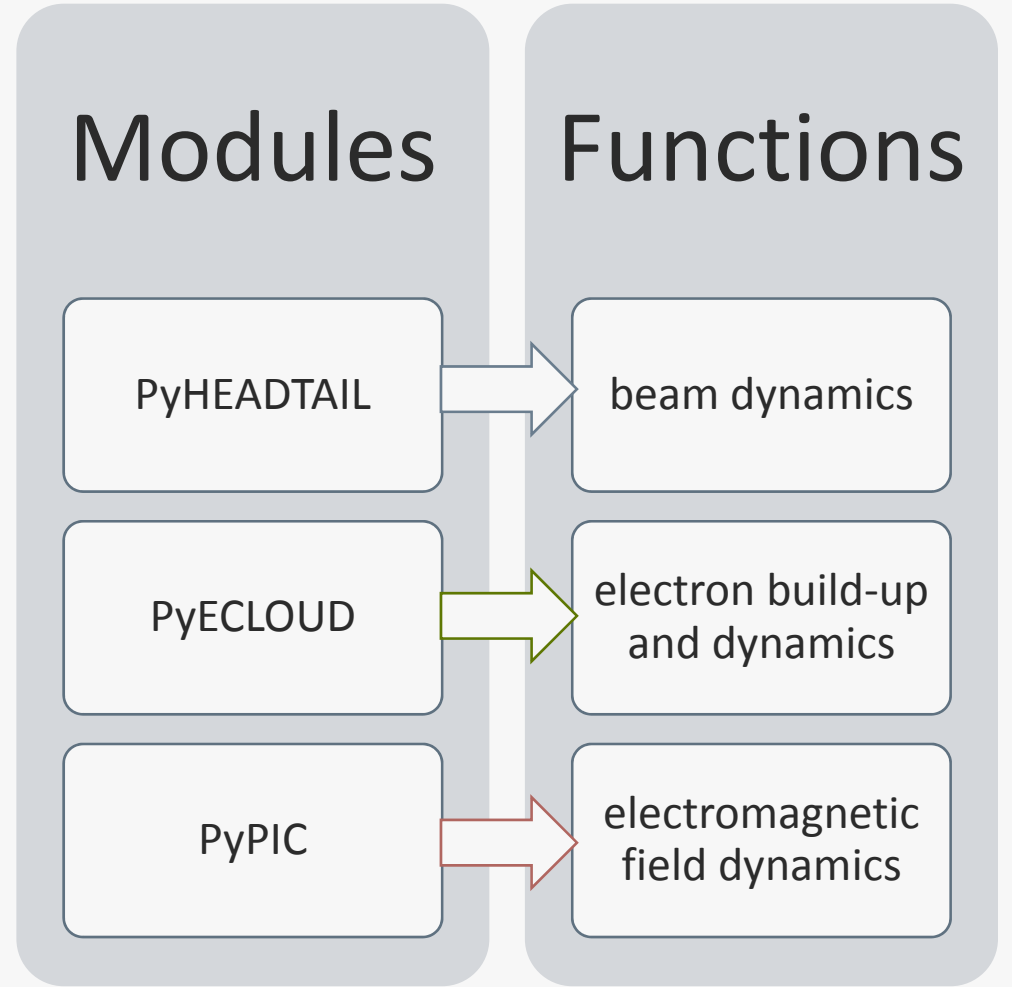
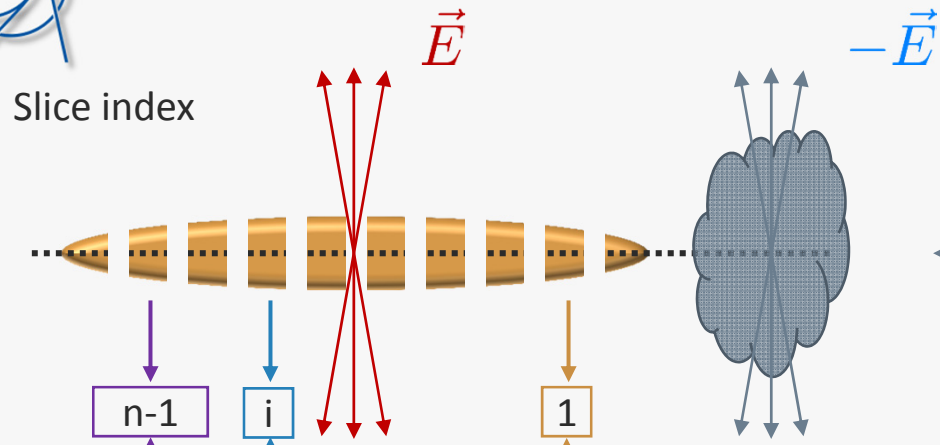


Courtesy
Giovanni Iadarola

Legend: From instability code – From build-up code – Interaction between the two codes

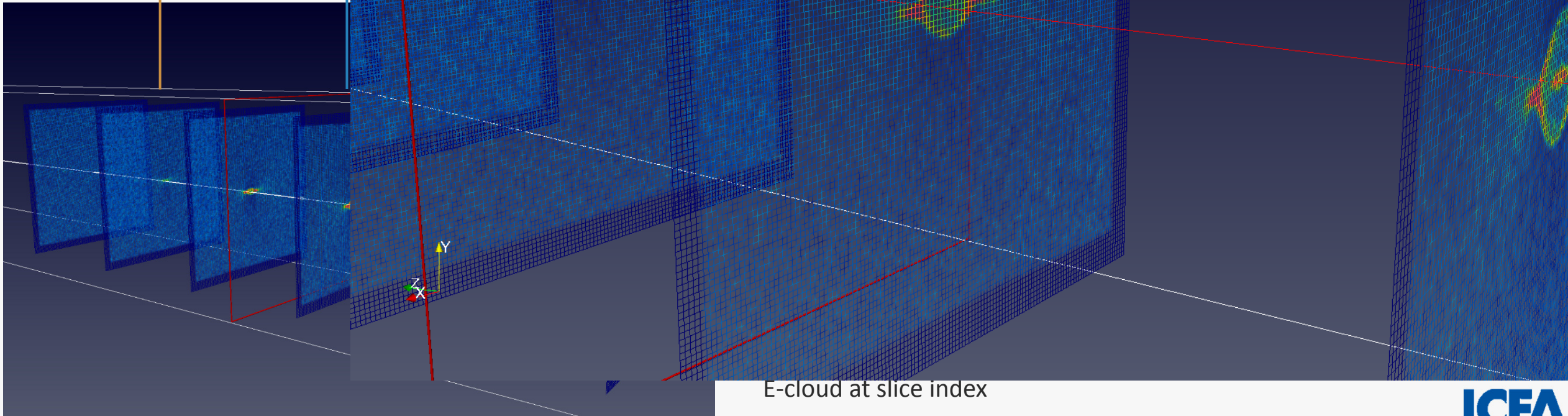
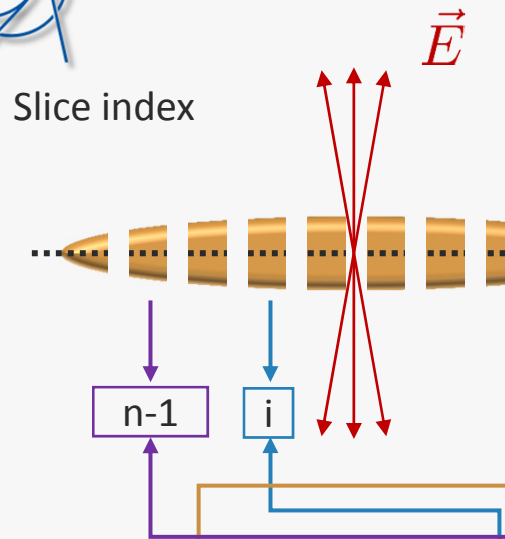


E-cloud beam system



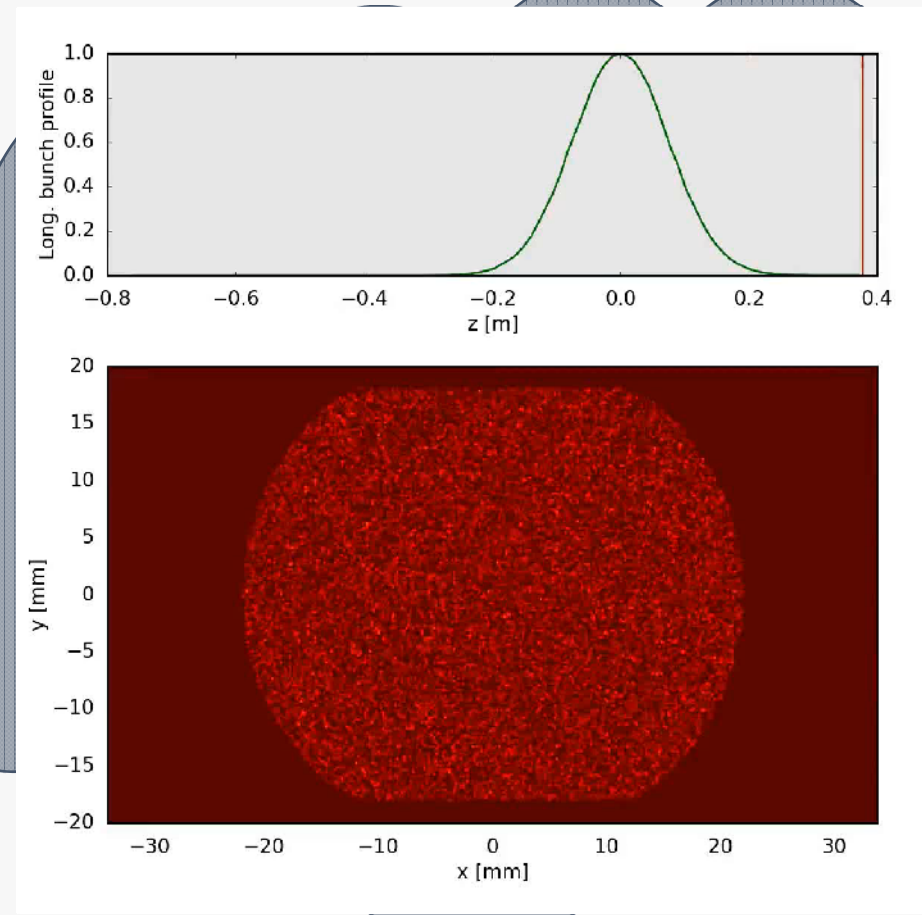
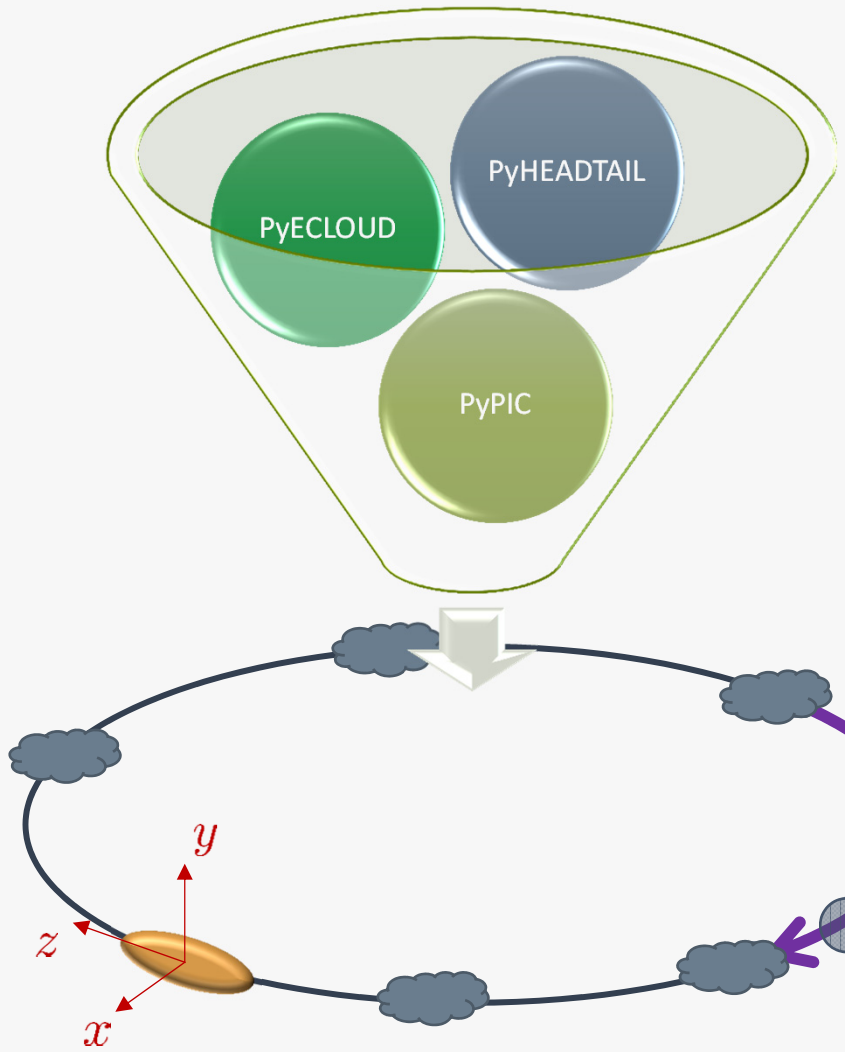
E-cloud at slice index





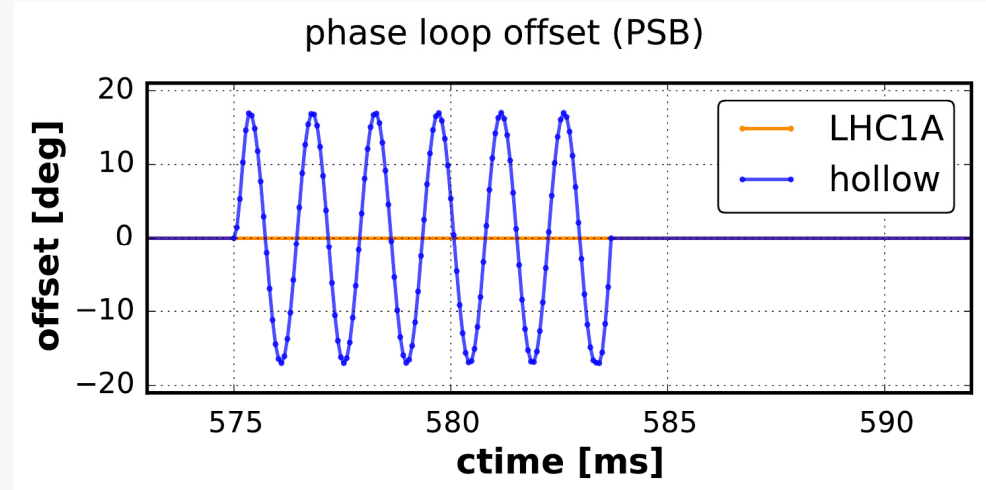
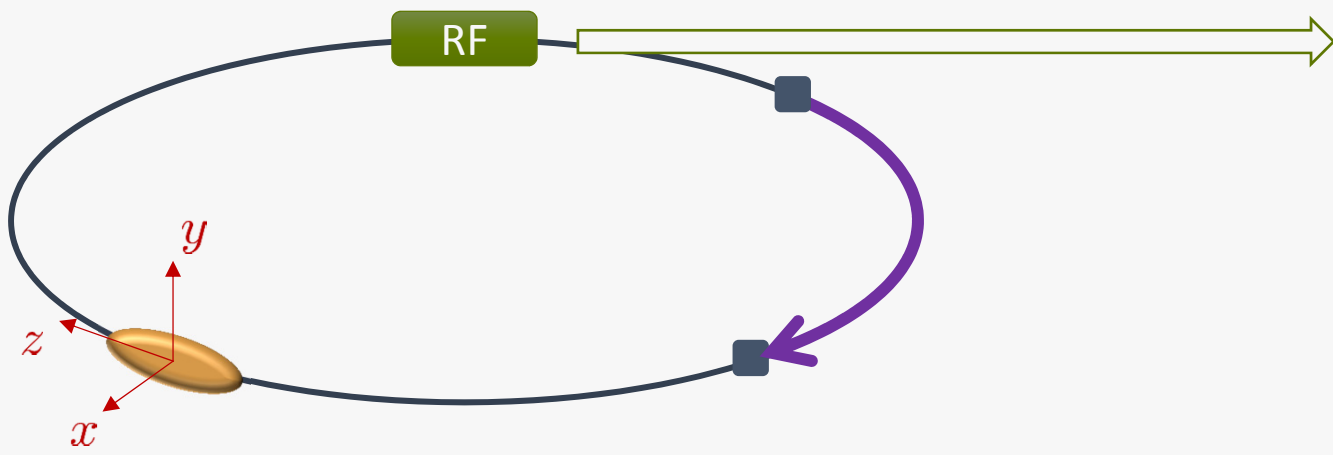
Electron clouds in a quadrupole magnet

- Two stream collective interaction – much more involved



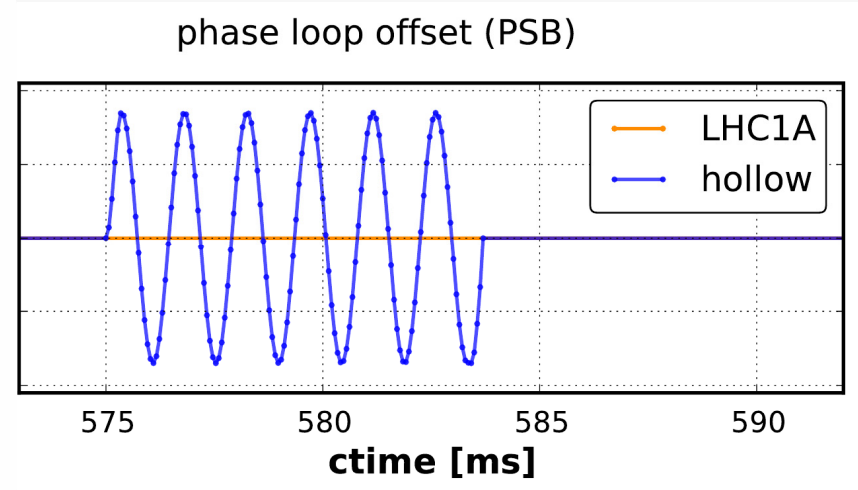
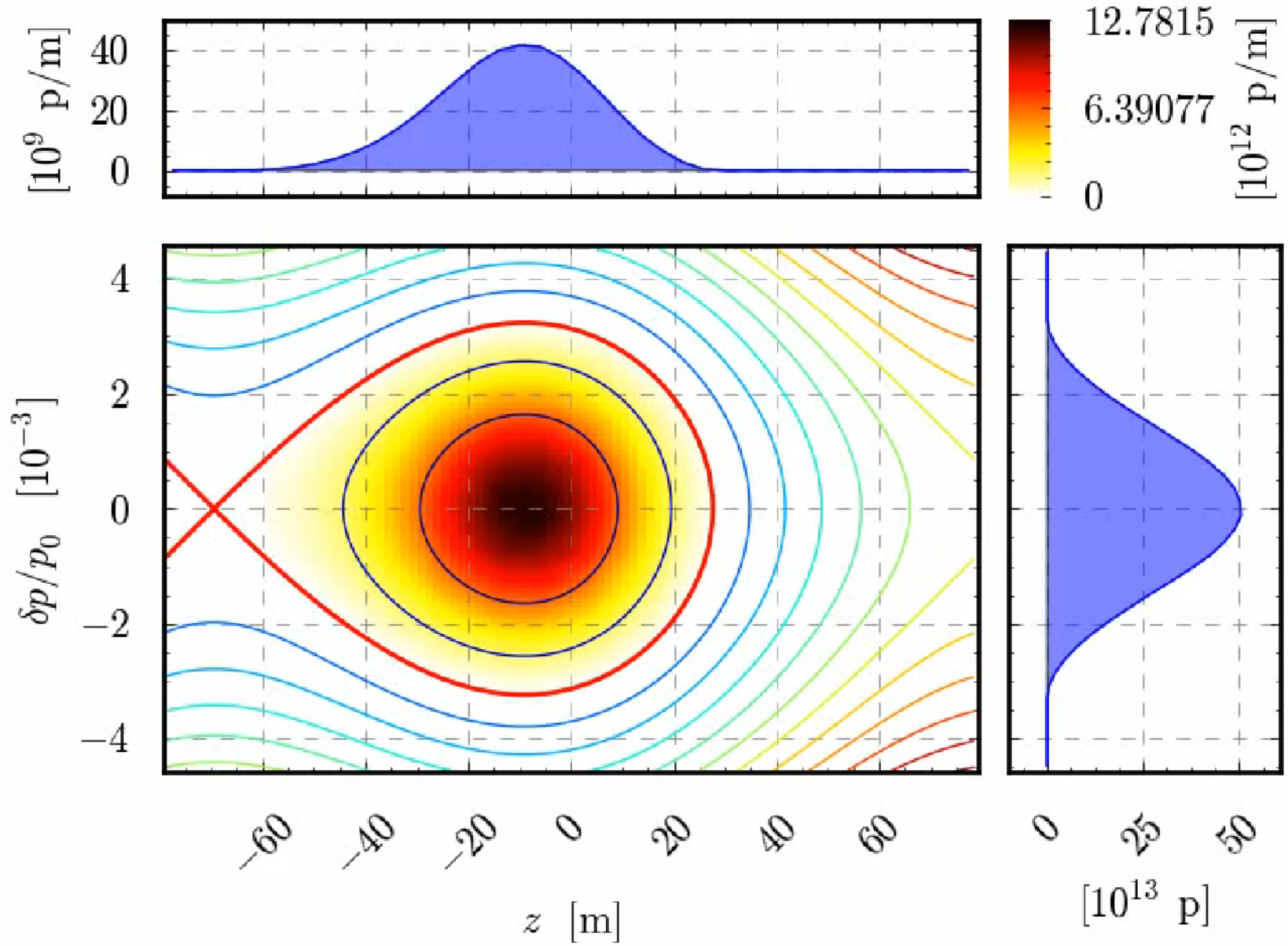
- Beam passage leads to a **pinch of the cloud** which in turn acts back on the beam – differently each turn

Trim function:
dynamically change property of RF
cavity



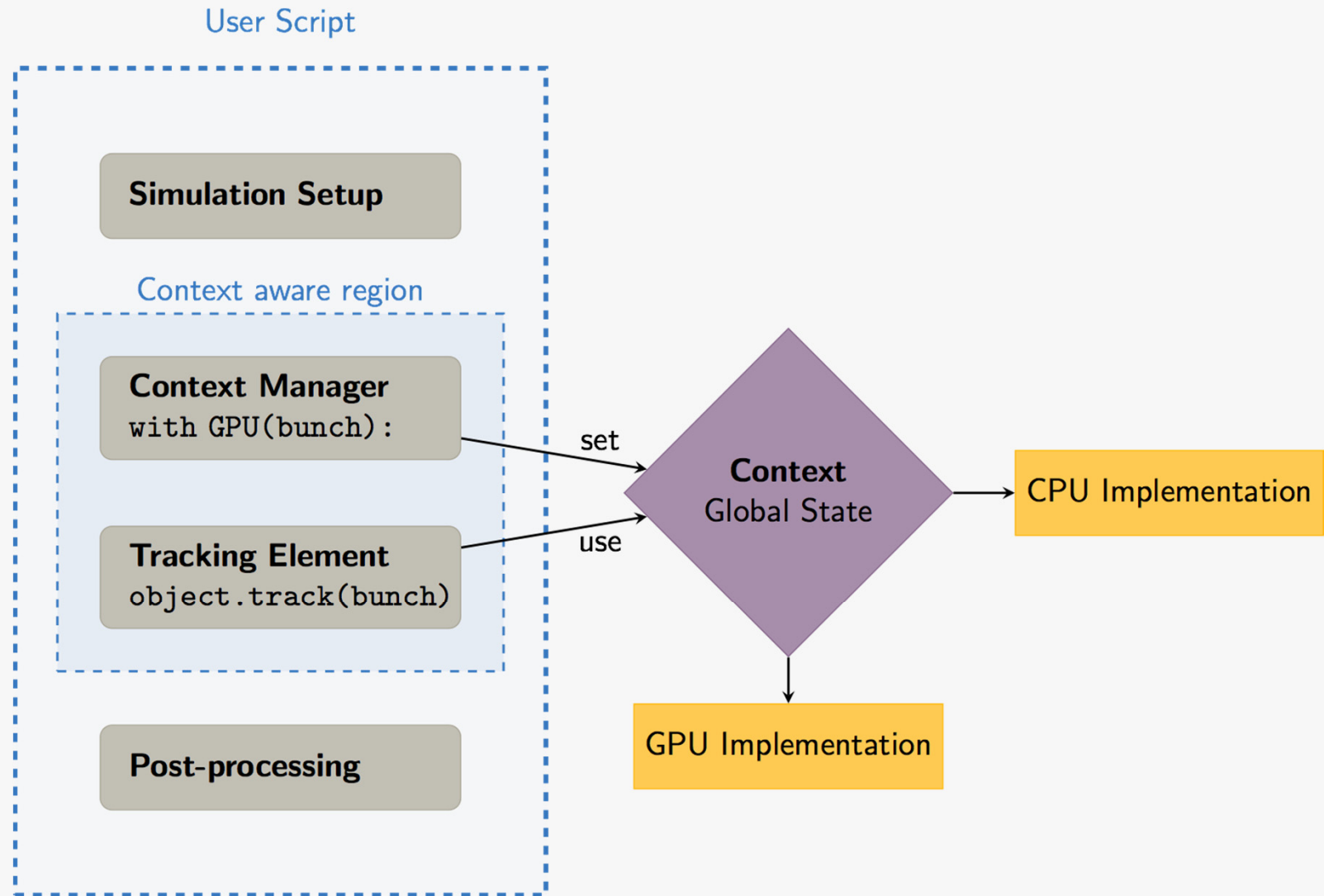
Hollow Bunches

Courtesy Adrian Oeftiger



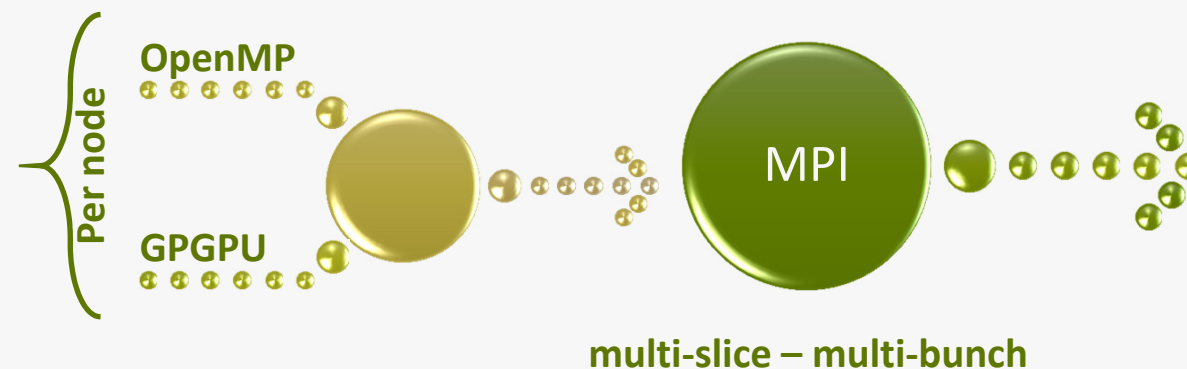
Context manager for GPU supported functions

1. Setup simulation
2. Set context with context manager
3. Track bunch: correct implementation automatically chosen
4. Move data back to CPU



A user does not need to care about the system internals

- Introduced collective effects and basic model of accelerator-beam systems used for simulations
- Highlighted some requirements for developers of modern computer simulation codes
- Highlighted the importance of performance and possibilities for improvement
- Showed some examples and applications
- Did not go into parallelisation techniques which **for collective effects become challenging**
- Parallelisation strategy would be to exploit all technics using a **hybrid approach**:



BACKUP

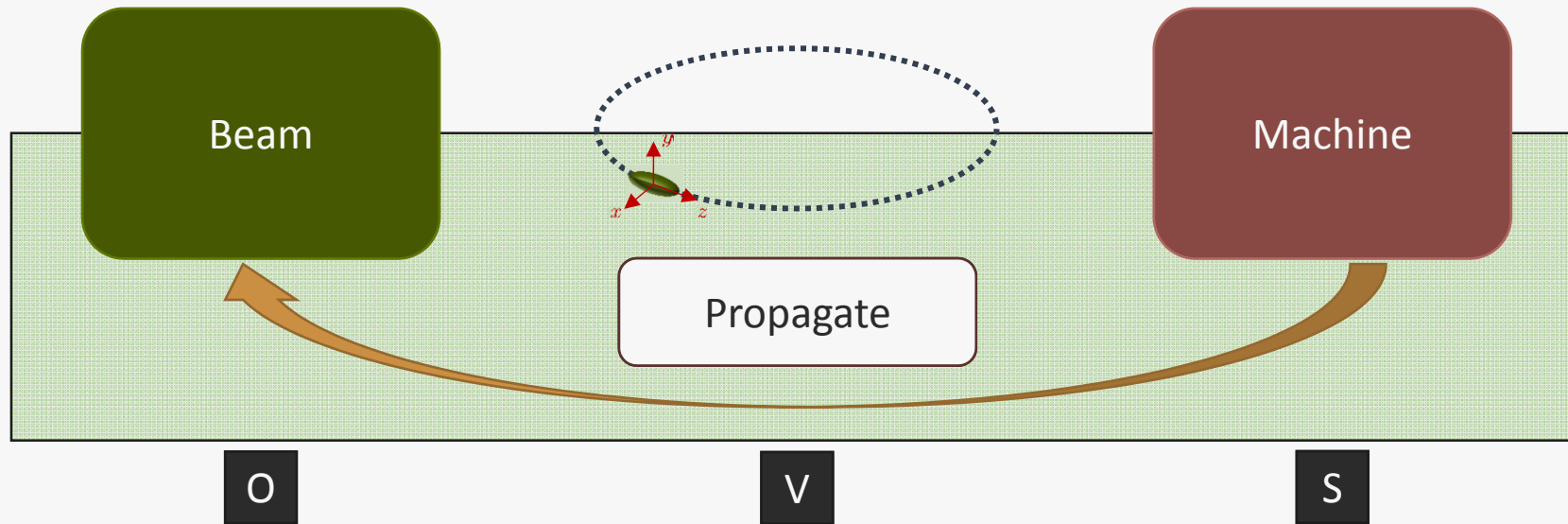
BACKUP

Outline:

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Mapping accelerator-beam to computer system

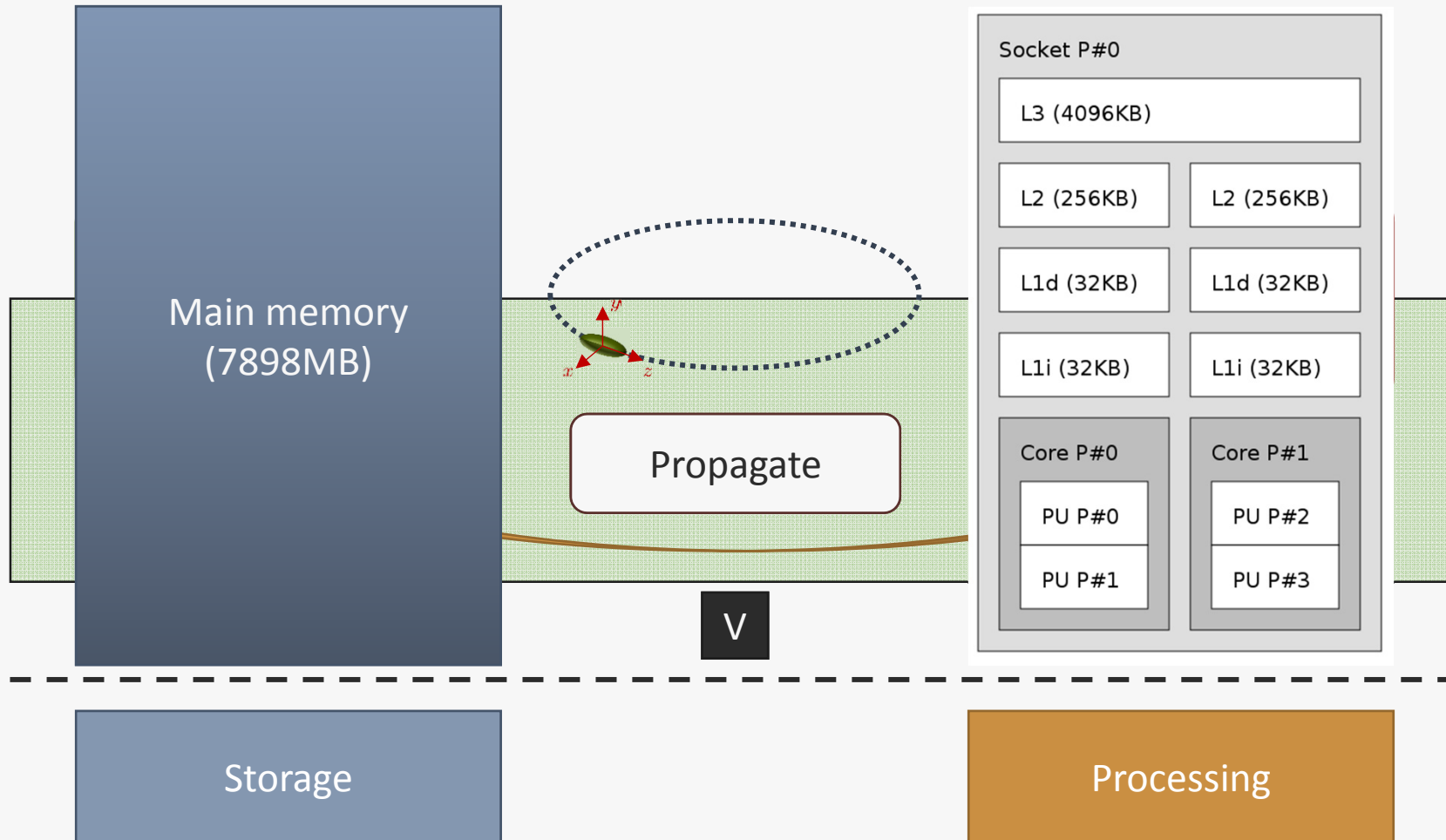
- Possible program layout





Mapping accelerator-beam to computer system

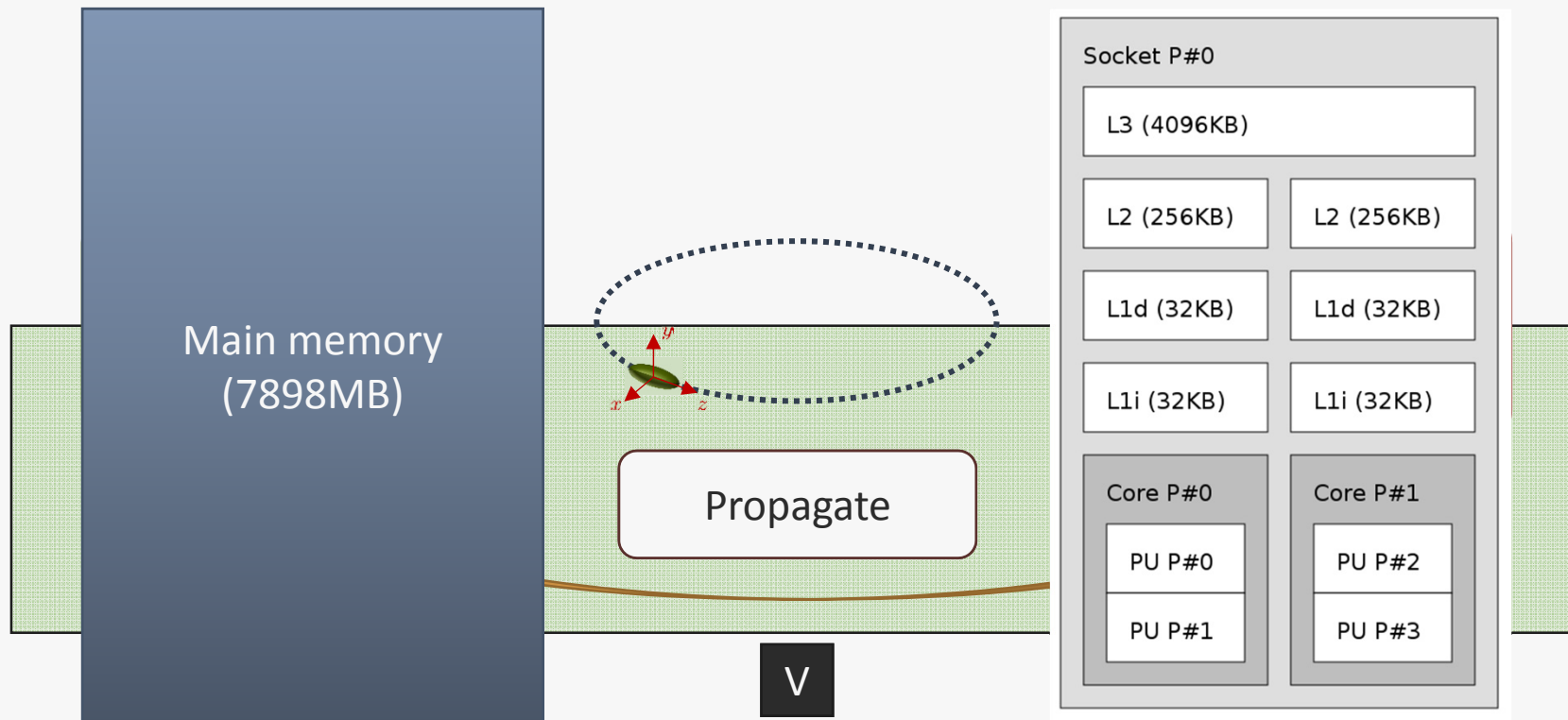
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Mapping accelerator-beam to computer system

- Possible program layout



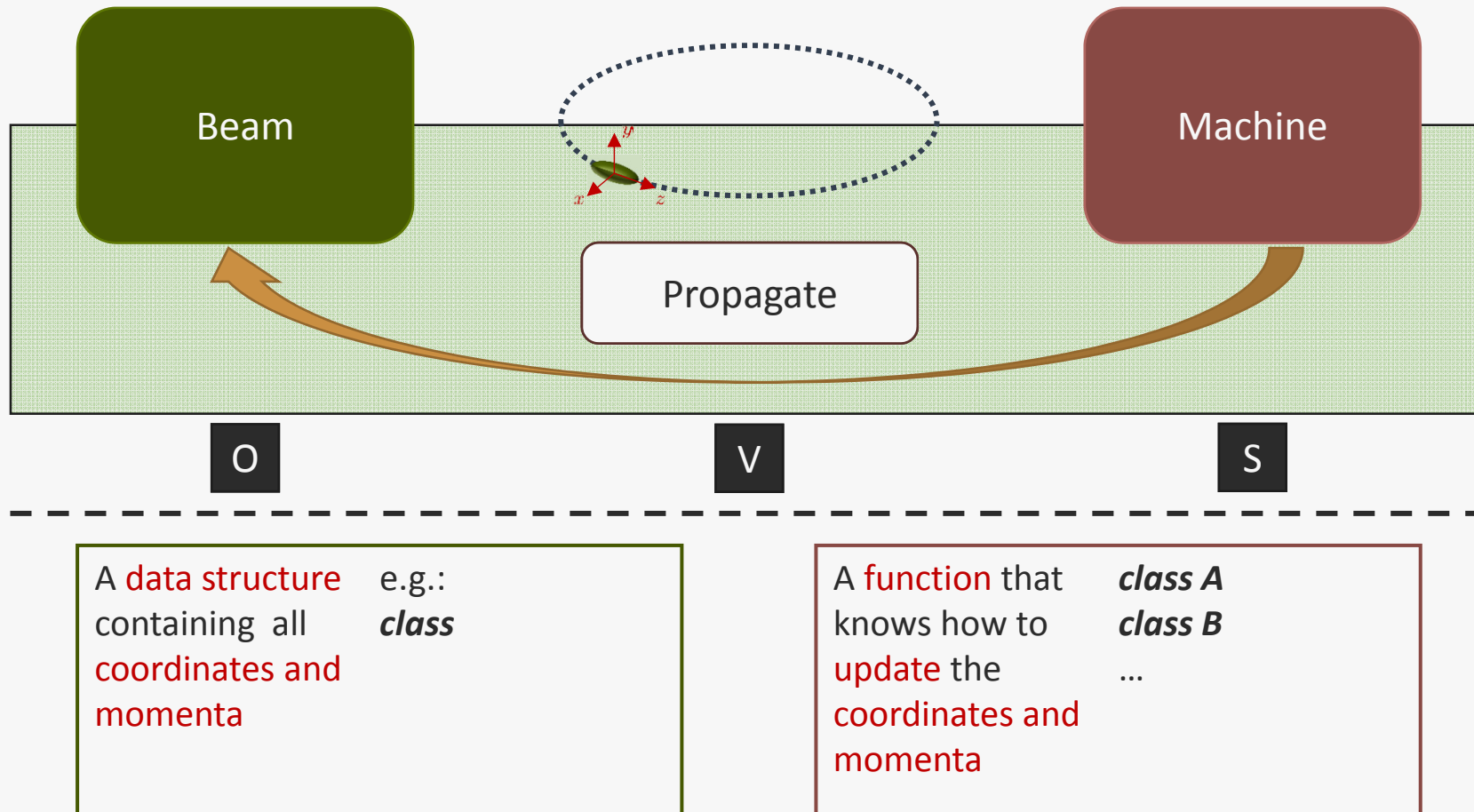
A **data structure** containing all **coordinates and momenta** e.g.: **class**

A **function** that knows how to **update the coordinates and momenta** **class A**
class B
...



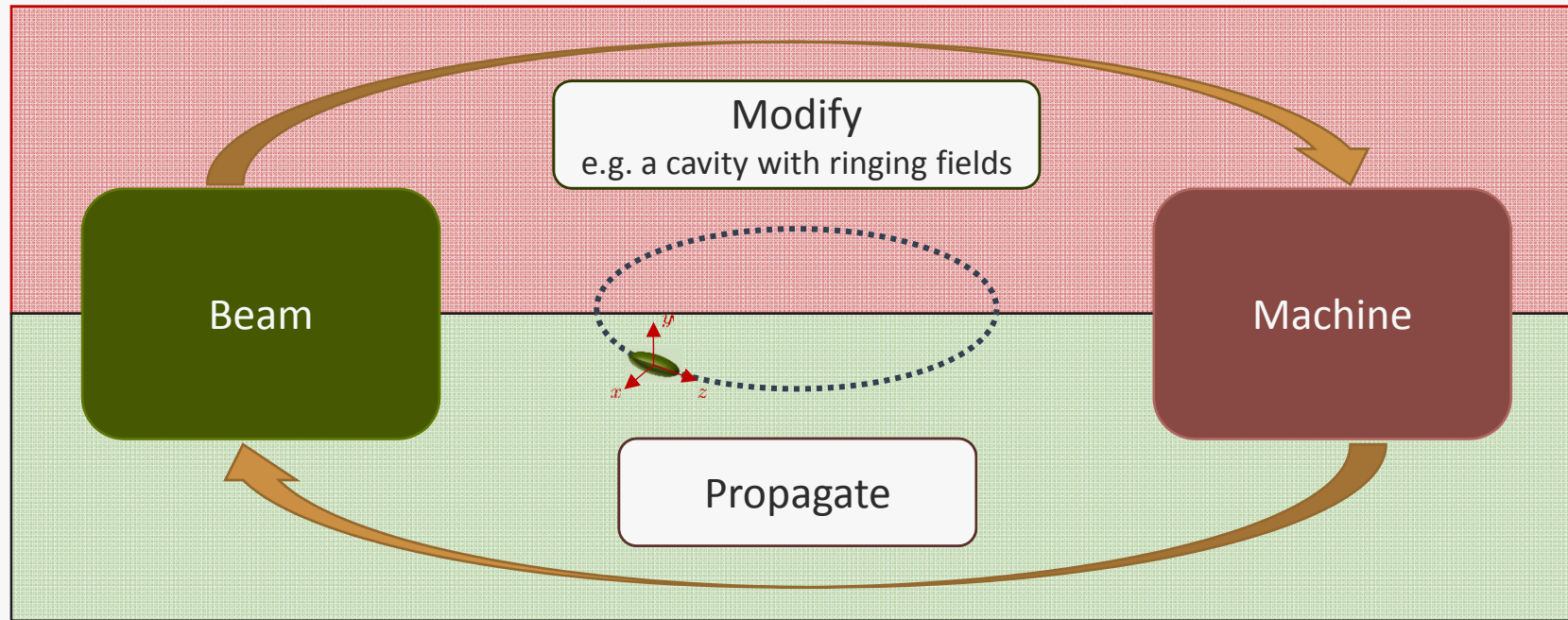
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Mapping accelerator-beam to computer system

- Possible program layout



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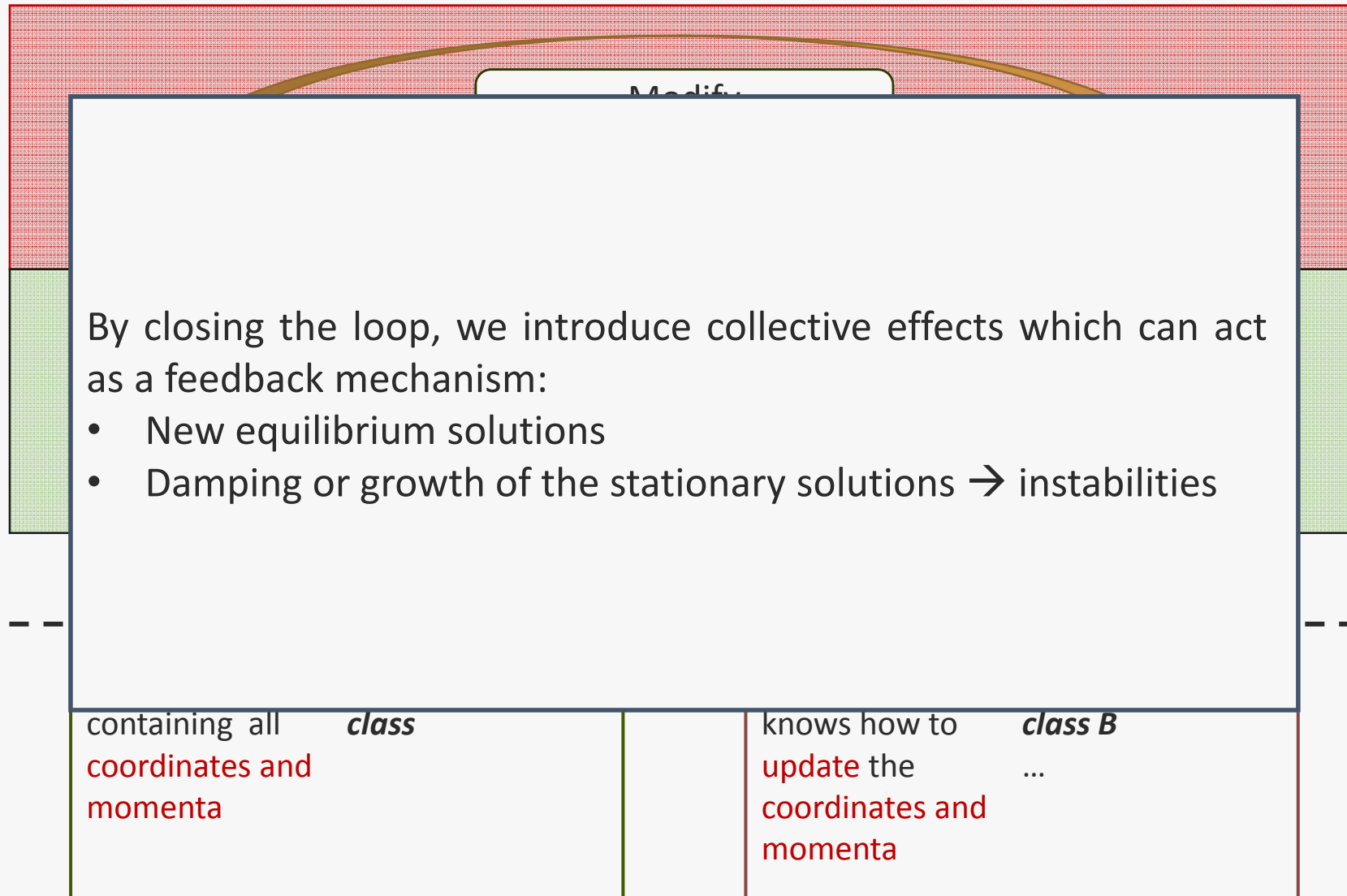
A **data structure** containing all **coordinates and momenta** e.g.: **class**

A **function** that knows how to **update the coordinates and momenta** **class A**
class B
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Mapping accelerator-beam to computer system

- Possible program layout

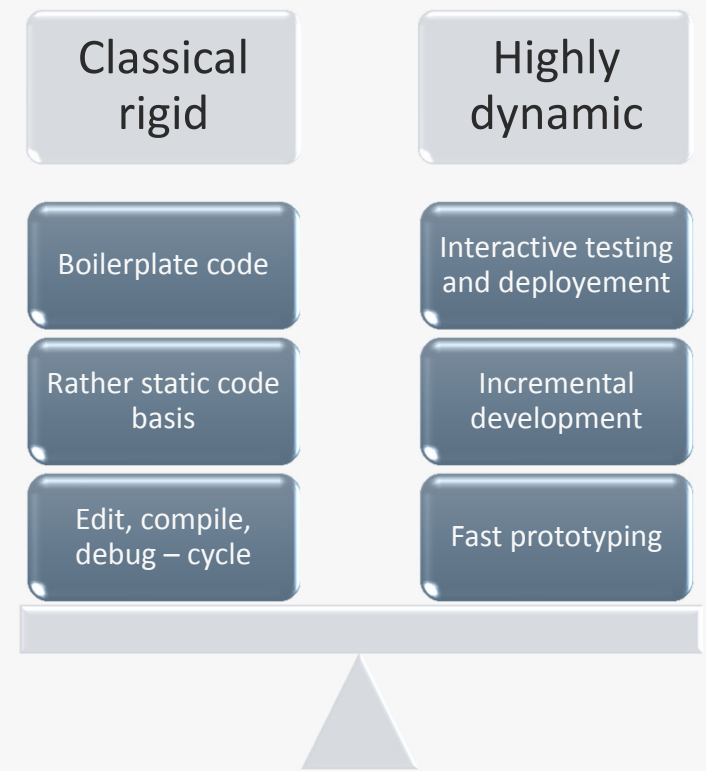
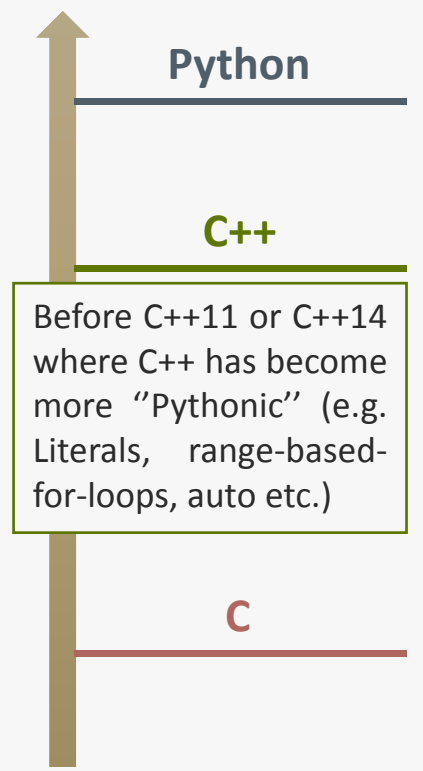


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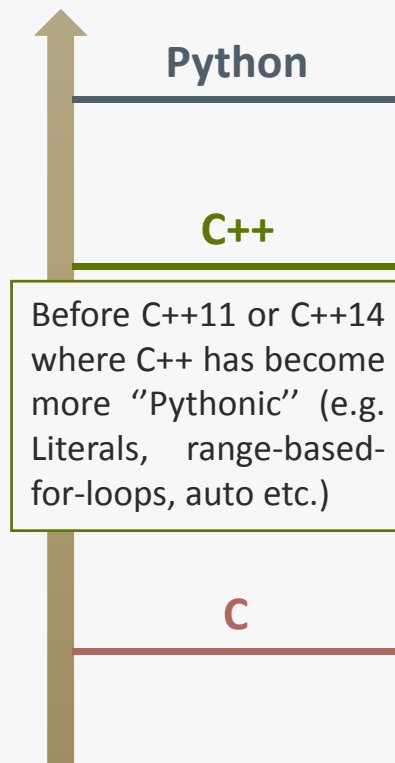
- We work today with **rapidly changing simulation** demands – this requires frequent and rapid code development which should preferably be **close to physics** rather than **close to the hardware**.

Abstraction (example)



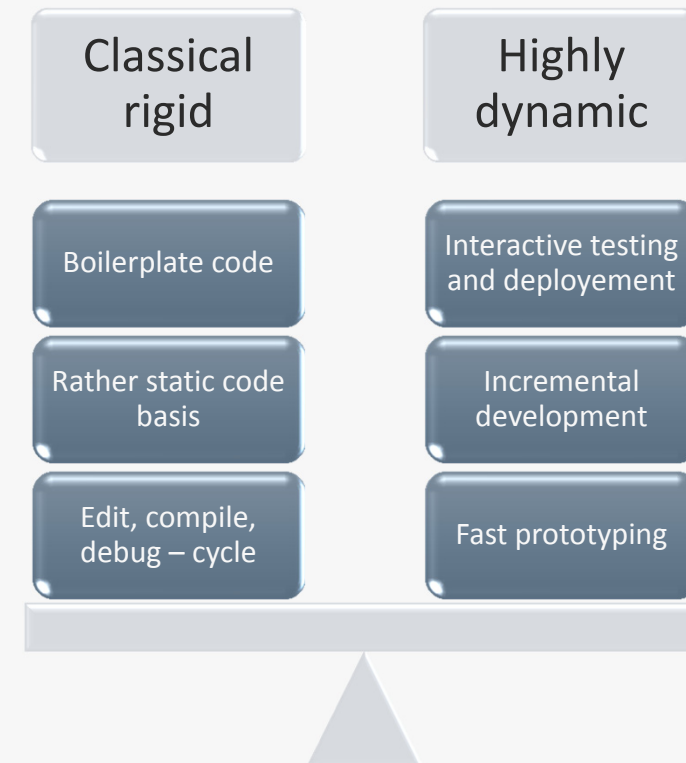
- We work today with **rapidly changing simulation** demands – this requires frequent and rapid code development which should preferably be **close to physics** rather than **close to the hardware**.

Abstraction (example)



Python is an object oriented **script language** while C++ is an object oriented **compiling language**.

Python code is ... often **5-10 times shorter** than equivalent C++ code! Anecdotal evidence suggests that one Python programmer can finish in two months what two C++ programmers can't complete in a year.



- We work today with **rapidly changing simulation** demands – this requires frequent and rapid code development which should preferably be **close to physics** rather than **close to the hardware**.

Abstraction (example)

An important hitch remains on the **FAST** requirement:

“Python was not made to be fast... .. but to make developers fast.”
Writing faster Python,
Sebastian Witowski


Being an interpreted language, strongly but dynamically typed, **Python can be slow in execution!** This needs to be handled.

- We work today with **rapidly changing simulation** demands – this requires frequent and rapid code development which should preferably be **close to physics** rather than **close to the hardware**.


Abstraction

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Coding. Crawler



Java

Python

```

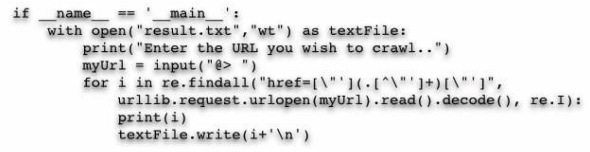

public class CrawlerExample {
    public static void main(String[] args) throws IOException {
        PrintWriter textFile = null;
        try {
            textFile = new PrintWriter("result.txt");
            System.out.println("Enter the URL you wish to crawl..");
            System.out.print("> ");
            String myUrl = new Scanner(System.in).nextLine();

            String response = getContentByUrl(myUrl);

            Matcher matcher = Pattern
                .compile("href=[\\\"'].{^\\\"'}+{\\\"'}").matcher(response);
            while (matcher.find()) {
                String url = matcher.group(1);
                System.out.println(url);
                textFile.println(url);
            }
        } finally {
            if(textFile != null) {
                textFile.close();
            }
        }
    }

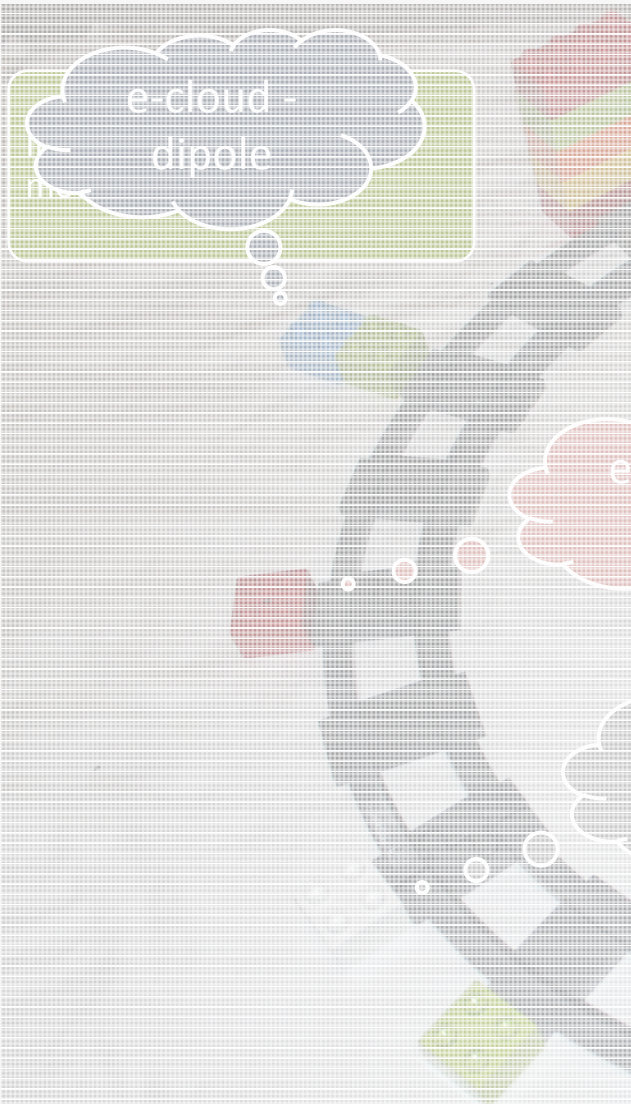
    private static String getContentByUrl(String myUrl)
        throws IOException {
        URL url = new URL(myUrl);
        URLConnection urlConnection = url.openConnection();
        BufferedReader in = null;
        StringBuilder response = new StringBuilder();
        try {
            in = new BufferedReader(new InputStreamReader
                (urlConnection.getInputStream()));
            String inputLine;
            while ((inputLine = in.readLine()) != null) {
                response.append(inputLine);
            }
        } finally {
            if(in != null) {
                in.close();
            }
        }
        return response.toString();
    }
}

```

Python,
Mitowski

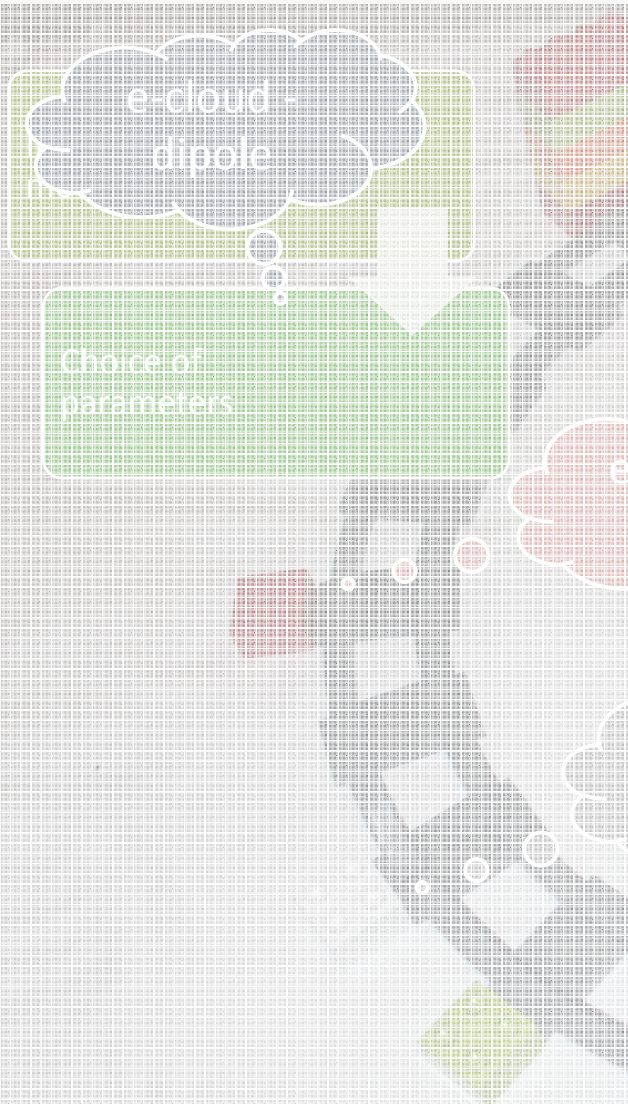
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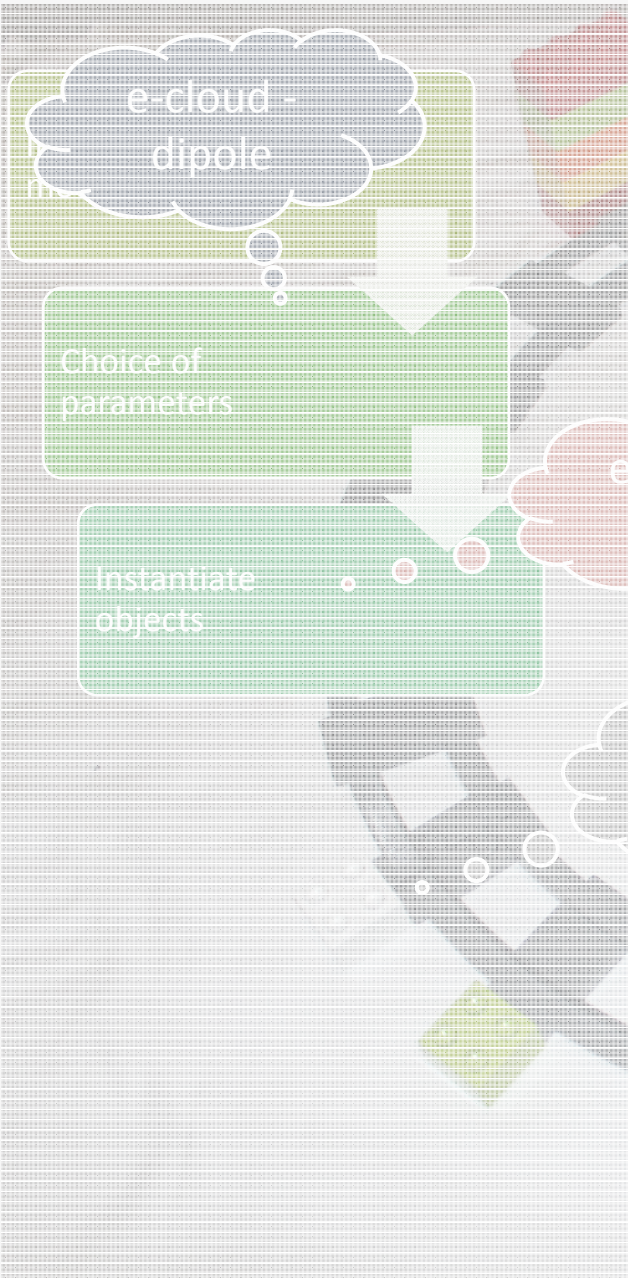
```

File Edit Options Buffers Tools Python Virtual Envs Elpy YASnippet Help
1 from __future__ import division
2
3 import time
4 import numpy as np
5 import seaborn as sns
6 import matplotlib.pyplot as plt
7 from scipy.constants import c, e, m_p
8
9 from PyHEADTAIL.trackers.rf_bucket import RFBucket
10 from PyHEADTAIL.particles.generators import ParticleGenerator
11 from PyHEADTAIL.particles.generators import gaussian2D, RF_bucket_distribution
12
13 from PyHEADTAIL.trackers.transverse_tracking import TransverseMap
14 from PyHEADTAIL.trackers.detuners import Chromaticity, AmplitudeDetuning
15
16 from PyHEADTAIL.trackers.simple_long_tracking import RFSystems
17
18 from PyHEADTAIL.particles.slicing import UniformBinSlicer
19 from PyHEADTAIL.impedances.wakes import CircularResonator, WakeField
20
21 from PyHEADTAIL.feedback.transverse_damper import TransverseDamper
22
23 from PyHEADTAIL.monitors.monitors import BunchMonitor, SliceMonitor
24
25
26 plt.switch_backend('TkAgg')
27 sns.set_context('talk', font_scale=1.5,
28               rc={'lines.markeredgewidth': 1})
29 sns.set_style('darkgrid', {
30     'axes.linewidth': 2,
31     'legend.fancybox': True})
32
33
34 # PARAMETERS
35 # =====
36 p0 = 7000e9 * e/c
37 E0 = p0*c
38 gamma = np.sqrt((p0/(m_p*c))**2 + 1)
39 beta = np.sqrt(1 - gamma**-2)
40 betagamma = np.sqrt(gamma**2 - 1)
41
42 C = 26658.883
43 R = C/(2*np.pi)
44 T0 = C/(beta*c)
45 omega0 = 2*np.pi/T0

```

```
File Edit Options Buffers Tools Python Virtual Envs Elpy YASnippet Help
33
34 # PARAMETERS
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36 p0 = 7000e9 * e/c
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38 gamma = np.sqrt((p0/(m_p*c))**2 + 1)
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40 betagamma = np.sqrt(gamma**2 - 1)
41
42 C = 26658.883
43 R = C/(2*np.pi)
44 T0 = C/(beta*c)
45 omega0 = 2*np.pi/T0
46 alpha = 53.86**-2
47 eta = alpha - gamma**-2
48
49 V_RF = [16e6, 0*8e6]
50 h_RF = [35640, 71280]
51 dphi_RF = [0, 0*np.pi]
52
53 macroparticlenumber = 50000
54 intensity = 1.3e11
55 epsn_x = 2.2e-6
56 epsn_y = 2.2e-6
57 epsn_z = 2.5
58
59 Q_x = 62.31
60 Q_y = 60.32
61 Qp_x = 0
62 Qp_y = 0
63 beta_x = R/Q_x
64 beta_y = R/Q_y
65
66
67 # PARTICLE DISTRIBUTION
68 # =====
69 rfbucket = RFBucket(
70     circumference=C, charge=e, mass=m_p, gamma=gamma,
71     alpha_array=[alpha], p_increment=0,
72     harmonic_list=h_RF, voltage_list=V_RF, phi_offset_list=dphi_RF)
73
74 bunch = ParticleGenerator(
75     macroparticlenumber=macroparticlenumber, intensity=intensity,
76     charge=e, mass=m_p, gamma=gamma, circumference=C,
77     distribution_x=gaussian2D(cpsn_x/betagamma), beta_x=beta_x
```



```

File Edit Options Buffers Tools Python Virtual Envs Elpy YASnippet Help
66
67 # PARTICLE DISTRIBUTION
68 # =====
69 rfbucket = RFBucket(
70     circumference=C, charge=e, mass=m_p, gamma=gamma,
71     alpha_array=[alpha], p_increment=0,
72     harmonic_list=h_RF, voltage_list=V_RF, phi_offset_list=dphi_RF)
73
74 bunch = ParticleGenerator(
75     macroparticlenumber=macroparticlenumber, intensity=intensity,
76     charge=e, mass=m_p, gamma=gamma, circumference=C,
77     distribution_x=gaussian2D(epsn_x/betagamma), beta_x=beta_x,
78     distribution_y=gaussian2D(epsn_y/betagamma), beta_y=beta_y,
79     distribution_z=RF_bucket_distribution(rfbucket, epsn_z=epsn_z)).generate()
80 bunch.x += 3.5e-4
81
82
83 # TRANSVERSE MAP
84 # =====
85 n_segments = 3
86
87 s = np.array([i * C/n_segments for i in range(n_segments + 1)])
88 alpha_x = np.zeros(n_segments + 1)
89 beta_x = np.ones(n_segments + 1) * beta_x
90 D_x = np.zeros(n_segments + 1)
91 alpha_y = np.zeros(n_segments + 1)
92 beta_y = np.ones(n_segments + 1) * beta_y
93 D_y = np.zeros(n_segments + 1)
94
95 detuners = [Chromaticity(Qp_x, Qp_y),
96             AmplitudeDetuning(-4e-9, 4e-9, -2e-10)]
97
98 transverse_map = TransverseMap(
99     s=s,
100     alpha_x=alpha_x, beta_x=beta_x, D_x=D_x,
101     alpha_y=alpha_y, beta_y=beta_y, D_y=D_y,
102     accQ_x=Q_x, accQ_y=Q_y,
103     detuners=detuners)
104 one_turn_map = [m for m in transverse_map]
105
106
107 # LONGITUDINAL MAP
108 # =====
109 longitudinal_map = RFSystems(
110     C, h_RF, V_RF, dphi_RF, [alpha, gamma, charge0, mass0, m_p])

```



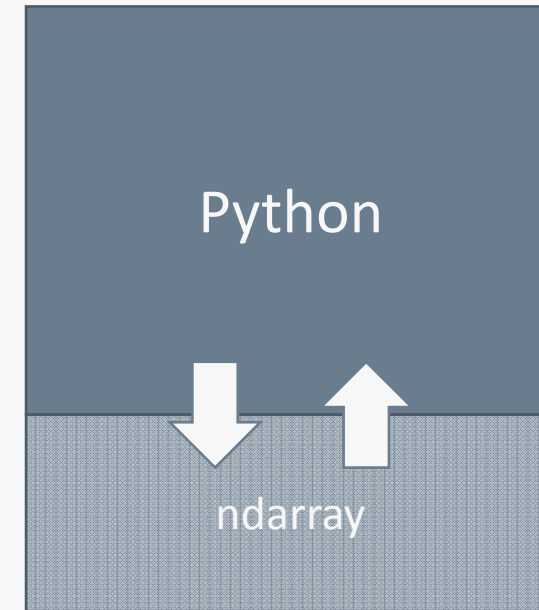
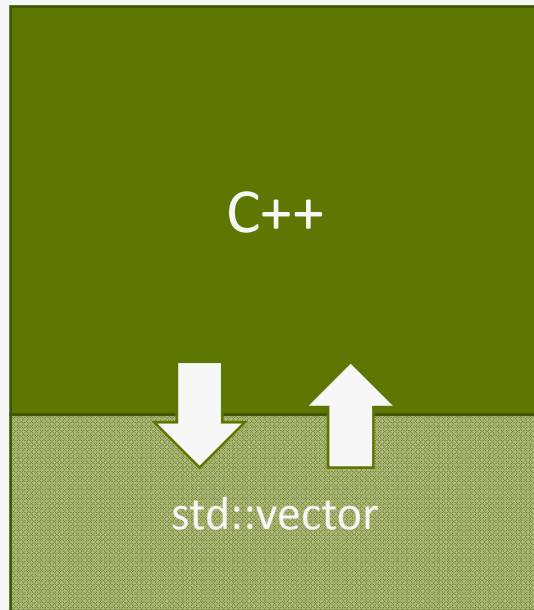
```
File Edit Options Buffers Tools Python Virtual Envs Elpy YASnippet Help
113
114 # CREATE WAKEFIELDS
115 # =====
116 slicer_for_wakefields = UniformBinSlicer(300, n_sigma_z=3)
117 wake = CircularResonator(R_shunt=1e6, frequency=700e6, Q=350, n_turns_wake=4)
118 wakefields = WakeField(slicer_for_wakefields, wake, circumference=C)
119
120
121 # CREATE DAMPER
122 # =====
123 dampingrate_x = 50
124 dampingrate_y = 50
125 damper = TransverseDamper(dampingrate_x, dampingrate_y)
126
127
128 # CREATE MONITORS
129 # =====
130 sigma_z = bunch.sigma_z()
131 slicer_for_slicemonitor = UniformBinSlicer(50, z_cuts=(-3*sigma_z, 3*sigma_z))
132 simulation_parameters_dict = {
133     'gamma': gamma,
134     'intensity': intensity,
135     'Qx': Q_x,
136     'Qy': Q_y,
137     'Qs': rfbucket.Qs,
138     'beta_x': bunch.beta_Twiss_x(),
139     'beta_y': bunch.beta_Twiss_y(),
140     'beta_z': rfbucket.beta_z,
141     'epsn_x': bunch.epsn_x(),
142     'epsn_y': bunch.epsn_y(),
143     'sigma_z': bunch.sigma_z(),
144 }
145 bunchmonitor = BunchMonitor('./bunchmonitor', 8192, simulation_parameters_dict)
146 slicemonitor = SliceMonitor('./slicemonitor', 8192, slicer_for_slicemonitor,
147                             simulation_parameters_dict)
148
149
150 # TRACKING LOOP
151 # =====
152 xx = np.linspace(-3e-3, 3e-3, 400)
153 yy = np.linspace(-3e-5, 3e-5, 400)
154 XX, YY = np.meshgrid(xx, yy)
155 JJ = -np.sqrt(XX**2 + (transverse_map.beta_x[0] * YY)**2)
156
157 zz = np.linspace(-6, 6, 400)
```

```
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166
167 s_cnt = 0
168 n_turns = 256
169 monitorswitch = False
170
171 print '\n--> Begin tracking...\n'
172
173 for i in range(n_turns):
174     t0 = time.clock()
175     for m in one_turn_map:
176         m.track(bunch)
177
178     bunchmonitor.dump(bunch)
179
180     if not monitorswitch:
181         if (bunch.mean_x() > 1e3 or bunch.mean_y() > 1e3 or i > n_turns-8192):
182             print "--> Activate monitor"
183             monitorswitch = True
184     else:
185         if s_cnt < 8192:
186             slicemonitor.dump(bunch)
187             s_cnt += 1
188
189     if (i+1) % 1 is not 0:
190         continue
191
192     Jx = np.sqrt((bunch.x-bunch.mean_x())**2 +
193                 (transverse_map.beta_x[0] * (bunch.xp-bunch.mean_xp()))**2)
194     ax1.contour(XX, YY, JJ, 6, lw=1)
195     ax1.scatter(bunch.x, bunch.xp, c=Jx, cmap=plt.cm.viridis_r, s=6)
196     ax2.contour(ZZ, PP, HH, 6, lw=1)
197     ax2.contour(ZZ, PP, HH, levels=[0], colors='darkred', lw=3)
198     ax2.scatter(bunch.z, bunch.dp, c=rfbucket.hamiltonian(bunch.z, bunch.dp),
199                cmap=plt.cm.viridis, s=6)
200     ax1.set_xlim(-1.3e-3, 1.3e-3)
201     ax1.set_ylim(-2e-5, 2e-5)
202     ax2.set_xlim(-.5, .5)
203     ax2.set_ylim(-5e-4, 5e-4)
204     ax1.set_xlabel("$x [m]$", fontsize=24)
205     ax1.set_ylabel("$x'$", fontsize=24)
206     ax2.set_xlabel("$z [m]$", fontsize=24)
207     ax2.set_ylabel("$\delta$", fontsize=24)
208     fig.suptitle("Turn# {:g}/{:g}".format(i+1, n_turns), fontsize=22)
209     plt.savefig('Movies/movie-{:03d}.png'.format(i+1), dpi=72)
210     # plt.draw()
```


Outline:

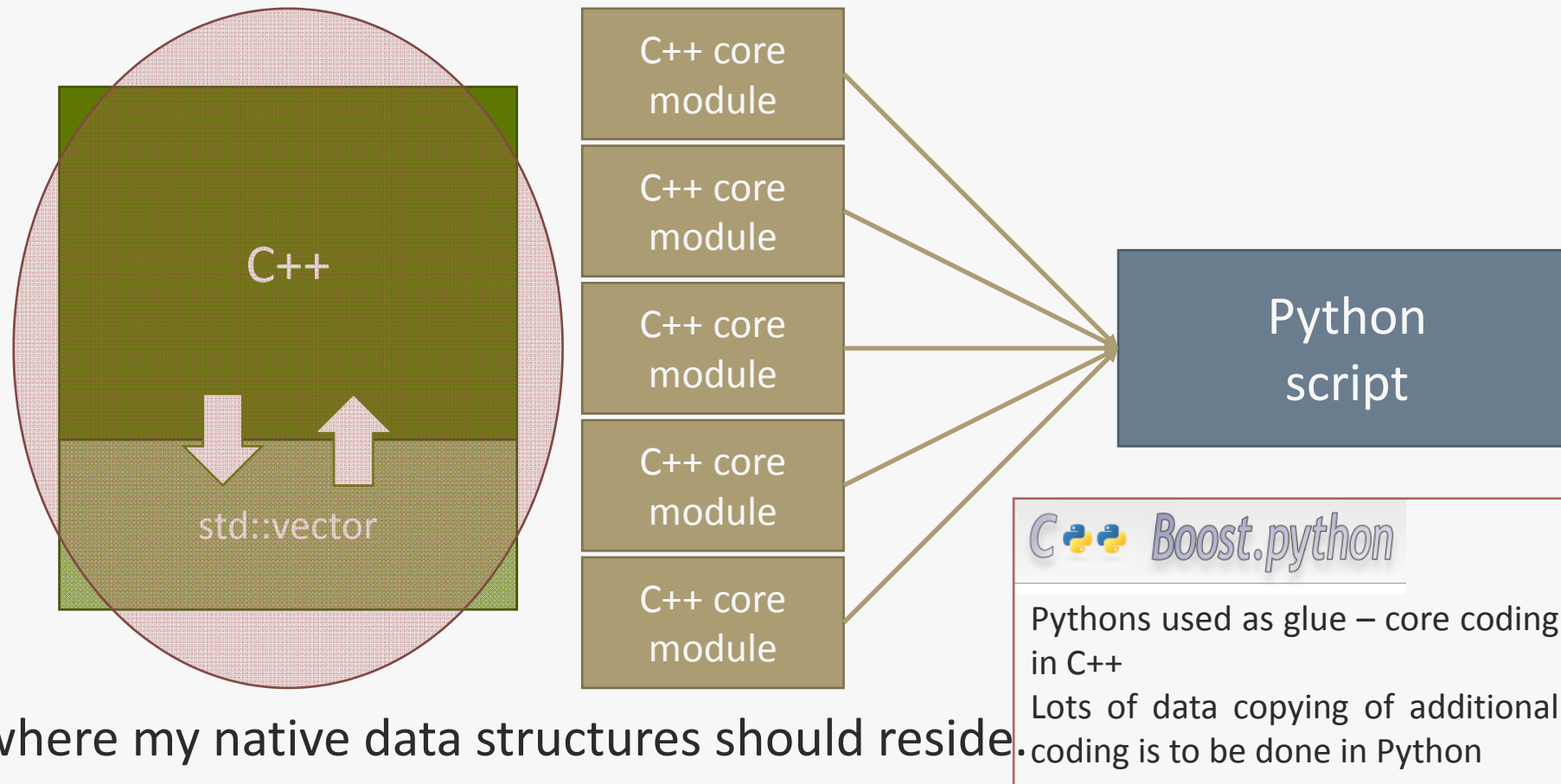
1. Introduction
2. Basic model of the accelerator-beam system
3. Modern approaches and program architectures
4. Performance considerations
5. Applications, present status and perspectives

Where do I want to spend most of my time coding in – in which world do I want to live?



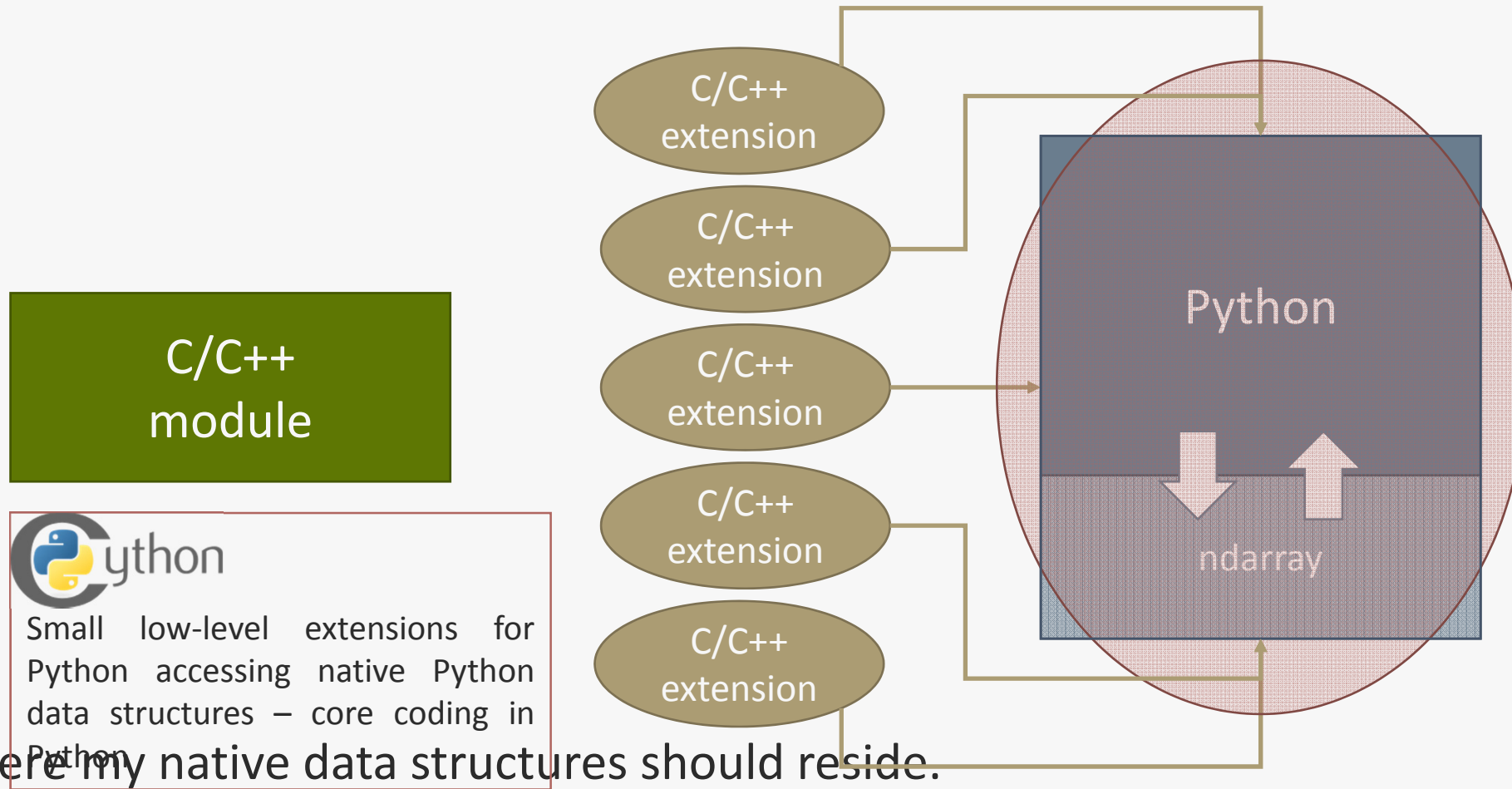
This is where my native data structures should reside.

Where do I want to spend most of my time coding in – in which world do I want to live?



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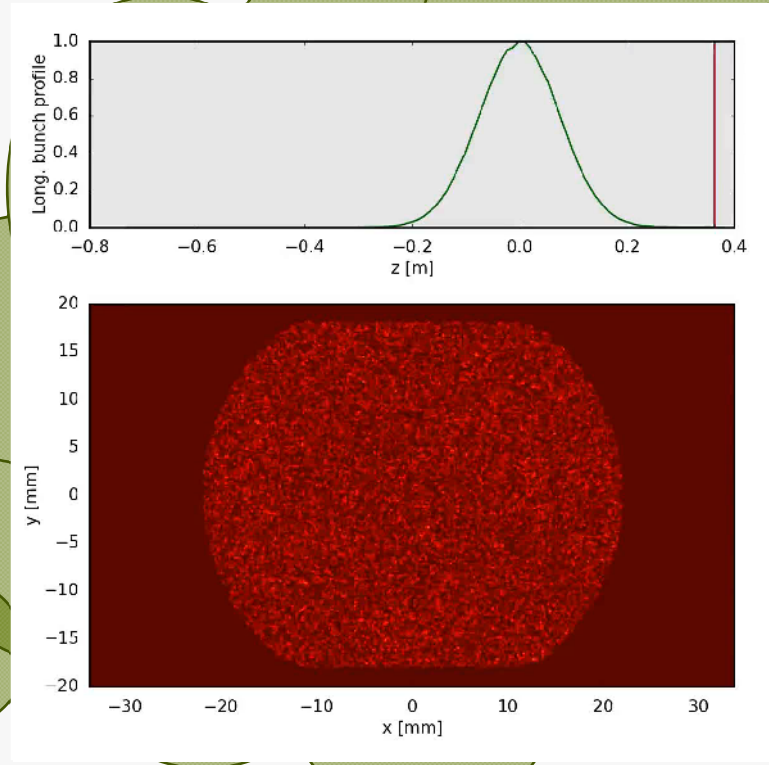
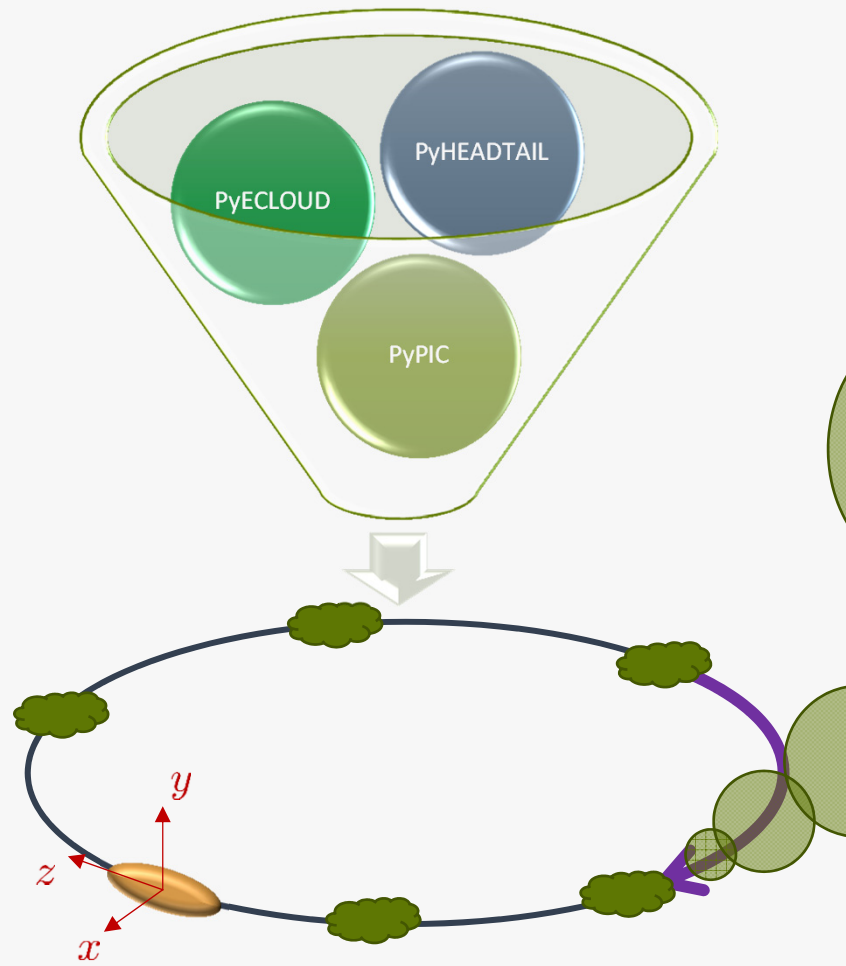


Outline:

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Electron clouds in a bending magnet

- Two stream collective interaction – much more involved



- Beam passage leads to a **pinch of the cloud** which in turn acts back on the beam – differently each turn

Typical application:

LHC@injection instability,
impedance + transverse damper

CPU Time: ~ 1day

GPU Time: 5x less

Two lines of code added to script

Benchmark for CPU

Results agree

